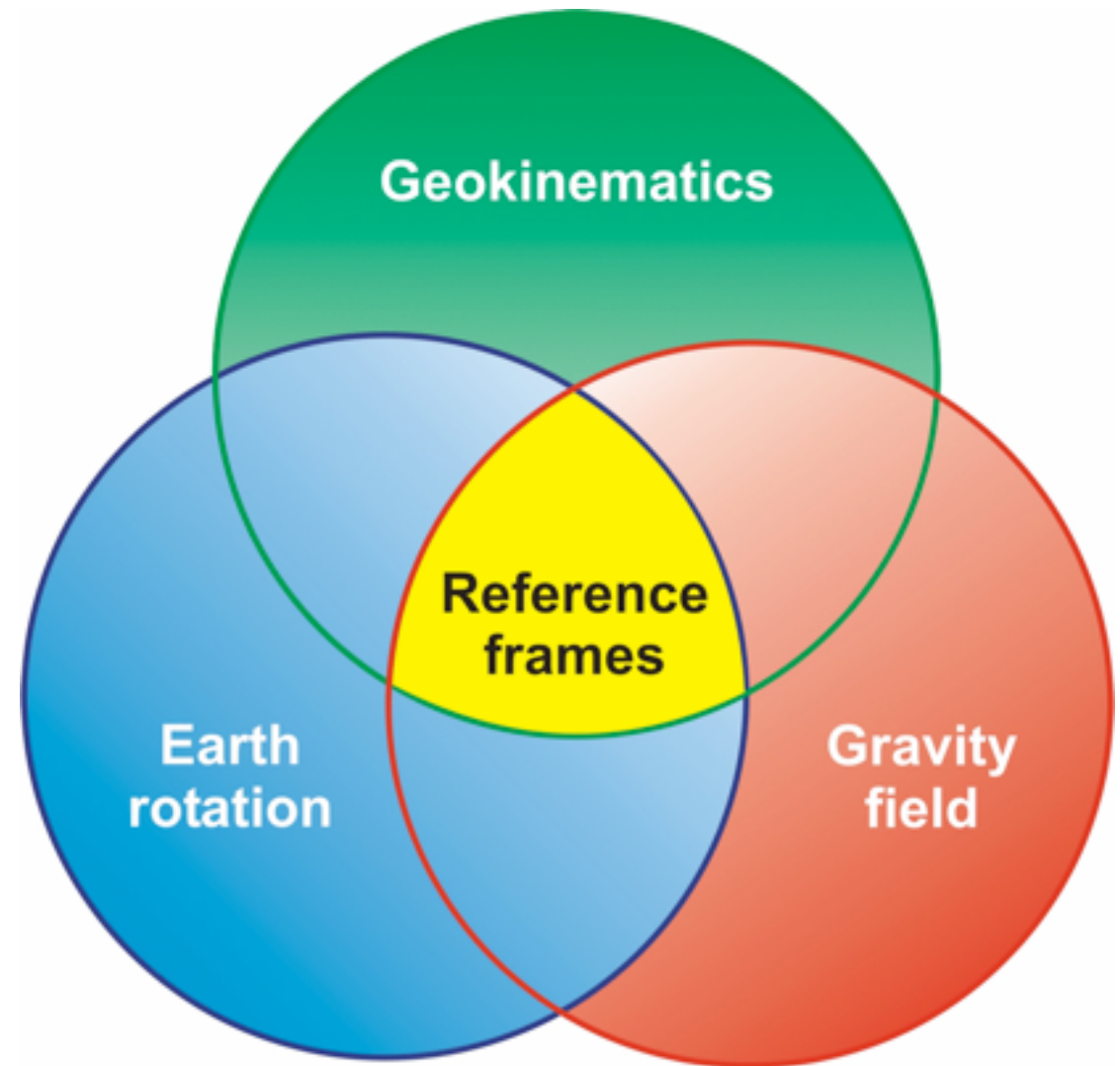


# Introduction: The Three Pillars of Geodesy

- Earth Shape (and how it changes over time)
- Earth Rotation
- Gravitational Field

*In this class:* We will focus on geometric aspects of Earth shape changes over time, and what they can tell us about for geophysical processes (mostly the solid Earth)



**The three pillars of geodesy.** *The changes in Earth's shape (geokinematic), gravity field and rotation, i.e. the "three pillars" of geodesy, provide the conceptual and observational basis for the reference frames required for Earth observation. Moreover, these "three pillars" are intrinsically linked to each other as they relate to the same unique Earth system processes. Today, the space-geodetic techniques and dedicated satellite missions are crucial in the determination and monitoring of geokinematics, Earth's rotation and the gravity field. Together, these observations provide the basis to determine the geodetic reference frames with high accuracy, spatial resolution and temporal stability.*



# THE GLOBAL GEODETIC OBSERVING SYSTEM

## Geodesy's contribution to Earth Observation



### GEODETIC OBSERVING SYSTEM (GGOS)

The Geodetic Observing System of the International Association of Geodesy (IAGG) was established by IAGG in July 2003. Since April 2003, IAGG represents IAGG in the Group on Earth Observation (GEO) and IAGG's contribution to the Global Earth Observation System (GEOSS).

### OBJECTIVE

International cooperation fostered by IAGG has led to the establishment of IAGG Services, that provide increasingly valuable observation products not only to scientists but also for a wide range of practical applications. Considering this development in geodesy, IAGG initially created GGOS as an IAGG Project during the IUGG 2003 in Sapporo, Japan. After the first two years devoted to the development of the internal organizational structure of GGOS and its integration with external organizations (the "Design Phase"), the Executive Committee of the IAGG at its meetings in August 2005 in Cairns, Australia, decided to continue the Project. In the "Implementation Phase" from 2005 to 2007, the GGOS Steering Committee, Executive Committee, Science Panel, Working Groups, and Web Pages were established. The Terms of Reference were revised. Finally, at the IUGG 2007 in Perugia, Italy, IAGG elevated GGOS to the status of a permanent observing system of IAGG.

### MEANINGS OF GGOS

Two very distinct aspects, which should not be confused: the "operational GGOS" consisting of components such as committees, working groups, etc., and the "observation system GGOS" comprising the infrastructure of many different instrument types, satellite and ground-based data and analysis centers. While GGOS as an organization established its structure from essentially new entities and will, in the next years, add new entities where needed, the observational system for GGOS as the system is being largely provided by the existing geodetic services.

### ORGANIZATION

The organization is a unifying umbrella for the IAGG Services and the interface between the Services and the "outside world". Inter-Service Committees, Science Panel and Working Groups focus on the most pressing issues relevant for all Services. The research needed to achieve the goals of GGOS influences the agenda of the IAGG Commission on Geodesy Working Groups. Externally, GGOS provides the links between IAGG Services and the main programs in Earth observations and geodesy. It constitutes a unique interface for many users to the IAGG Services. In particular, GGOS participates on behalf of IAGG in international programs focusing on Earth observations.

According to the IAGG By-Laws, GGOS "works with the IAGG Services and Commissions to provide the geodetic infrastructure necessary for the study of the Earth system and global change research." This implies a vision and a mission for GGOS. The implicit vision is to empower Earth science to extend our knowledge and understanding of the Earth system processes, to monitor ongoing changes and to increase our capability to predict the future behavior of the system. Likewise, the embedded mission is to facilitate the exchange of information among the IAGG Services and Commissions and other stakeholders in the Earth science and Earth Observation communities, to provide scientific advice and coordination that will enable the IAGG to develop products with higher accuracy and consistency and to meet the requirements of particularly global change research, and to ensure the accessibility of geodetic observations and products for the benefit of users. The IAGG Services, upon which GGOS is built, are organized as a framework for communication, coordination, and scientific advice necessary to develop improved or new products with higher accuracy, consistency, resolution, and stability. IAGG sees GGOS as an agent to improve the visibility of geodesy's contribution to the Earth sciences and to society in general. The users, both individual members of IAGG, benefit from GGOS as a single point of contact for the global geodetic observation system of systems maintained by IAGG Services not only for the access to products but also to the expertise. Society benefits from GGOS as a utility supporting national and global Earth observation systems as a basis for information and decision-making.

### GGOS THE OBSERVING SYSTEM

GGOS as an observing system is built upon the existing and future infrastructure provided by the IAGG Services. It aims to provide consistent observations of the spatial and temporal changes of the shape and gravitational field of the Earth, as well as the temporal variations of the Earth's rotation. In other words, it aims to deliver a global picture of the surface kinematics of our planet, including the ocean, ice cover and land surfaces. In addition, it aims to deliver estimates of mass anomalies, mass transport and mass exchange in the Earth system. Surface kinematics and mass transport together are the key to global mass balance determination, and an important contribution to the understanding of the energy budget of our planet. Moreover, the system aims to provide the observations that are needed to determine and maintain a terrestrial reference frame of higher accuracy and greater temporal stability than what is available today. By combining the "three pillars" into one observing system having utmost accuracy and operating in a well-defined and reproducible global terrestrial frame, GGOS adds to these pillars a new quality and dimension in the context of Earth system research. The observing system, in order to meet its objectives, has to combine the highest measurement precision with spatial and temporal consistency and stability that is maintained over decades.

### GGOS AND ITS CHALLENGES

The observing system GGOS faces two types of scientific and technological challenges:

1. GGOS and the geodetic technologies need to meet the demanding user requirements in terms of reference frame accuracy and availability, as well as in terms of spatial and temporal resolution and accuracy of the geodetic observations. Developing an observing system capable of measuring variations in the Earth's shape, gravity field, and rotation with an accuracy and consistency of 0.1 to 1 ppb, with high spatial and temporal resolution, and increasingly low time latency, is a very demanding task. Accommodating the transition of new technologies as they evolve in parallel to maintaining an operational system is part of this challenge.
2. The Earth system is a complex system with physical, chemical and biological processes interacting on spatial scales from micrometers to global and temporal scales from seconds to billions of years. The integration of the "three pillars" into a system providing information on mass transport, surface deformations, and dynamics of the Earth therefore requires a "whole Earth" approach harnessing the expertise of all fields of Earth science.

### GGOS: AN OBSERVING SYSTEM OF LAYERED INFRASTRUCTURE

GGOS as an observing system has five major levels of instrumentation and objects that actively perform observations, are passively observed, or both. These levels are:

- Level 1: the terrestrial geodetic infrastructure;
- Level 2: the LEO satellite missions;
- Level 3: the GNSS and the Lageos-type SLR satellites;
- Level 4: the planetary missions and geodetic infrastructure on Moon and planets;
- Level 5: the extragalactic objects.

These five levels of instrumentation and objects, independent of whether they are active or passive, receivers or emitters or both, are connected by many types of observations in a rather complex way to form the integrated GGOS observing system. In this system, the major observation types at present are:

1. observations of the microwaves at the ground and at the LEO satellites emitted by GNSS satellites;
2. laser ranging to LEOs, dedicated laser ranging satellites, GNSS satellites and the Moon;
3. microwave observation of extragalactic objects (quasars) by VLBI;
4. instrumentation onboard the LEO satellites measuring accelerations, gravity gradients, satellite orientation, etc.;
5. radar and optical observations of the Earth's surface (land, ice, glaciers, sea level, etc.) from remote sensing satellites;
6. distance measurements between satellites (K-band, optical, interferometry, etc.).

In the future, new measurement techniques will evolve and be included into the system. Different parts of the overall system are cross-linked through observations and inter-dependent. All these techniques are affected by and measure the "output" of the same unique Earth system, that is, the various geodetic fingerprints induced by mass redistribution and changes in the system's dynamics. Therefore, consistency of data processing, modeling, and conventions across the techniques and across the "three pillars" is mandatory for maximum exploitation of the full potential of the system.

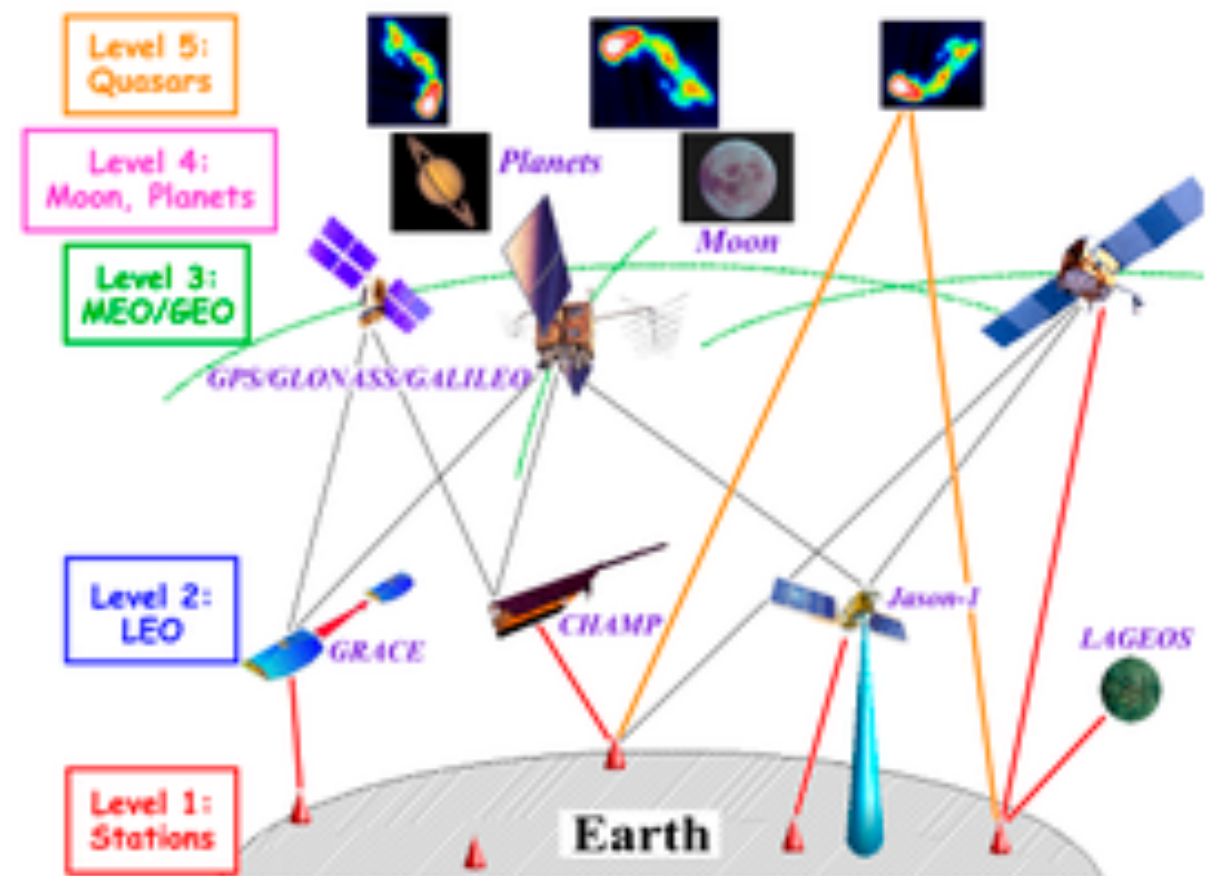
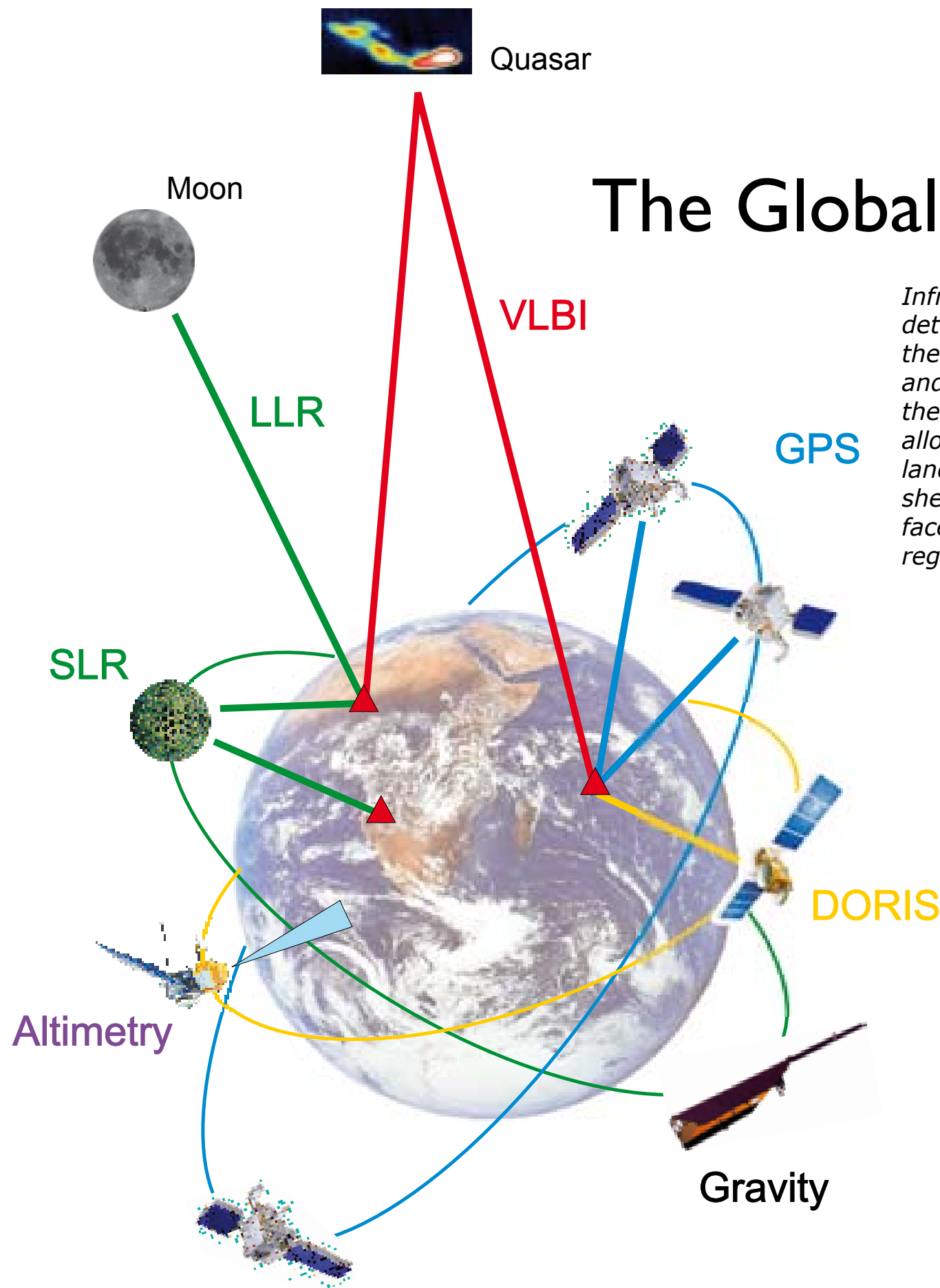




# GGOS

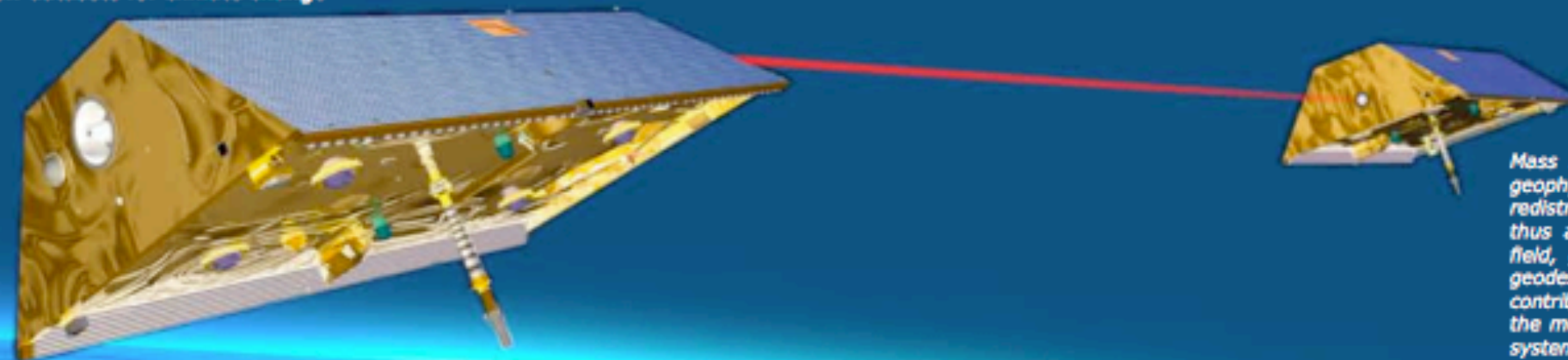
## The Global Geodetic Observing System

Infrastructure contributing to GGOS. The combined infrastructure allows the determination and maintenance of the global geodetic reference frames, and the determination of Earth's gravity field and rotation. The ground networks and navigation satellites (currently GPS) are crucial for maintaining the reference frame required for high accuracy positioning. In particular, they allow the monitoring of volcanoes, earthquakes, tectonically active regions and landslide-prone areas. The Low Earth Orbit (LEO) satellites monitor sea level, ice sheets, water storage on land, atmospheric water content, high-resolution surface motion, and variations in the Earth's gravity field. The latter are caused by regional and global mass transport processes as, e.g., the hydrological cycle.





... laser-ranging targets. The innovative sensor technologies used in these gravity field missions have already enabled a dramatic improvement of the gravity field during the last decade. Gravity field models derived from GRACE have benefited the space geodetic analysis of the DORIS ranging data. They have been used to improve the knowledge of the Earth's geoid from ocean radar altimetry satellites, and for laser altimeters, thus enhancing the geodetic contributions from other space missions. Gravity missions are also of central importance for altimetry, because a precise geoid is required to refer the sea surface topography to the Earth's mean sea level. The integration of all the satellite missions with the existing space geodetic techniques for the determination of the Earth's shape opens new opportunities to determine and study the mass transport in the Earth system in a globally consistent way or to derive information on changes in part of the water cycle. Analysis of the data delivered by GRACE yields a direct measure of mass flux with high spatial resolution (about 500 km on the Earth's surface, and sub-monthly temporal resolution). Combining these mass changes with advanced meteorological models is predicting water storage on land such as the Global Land Data Assimilation System (GLDAS) rapidly improves the quantitative knowledge of the water cycle and provides new datasets for climate change studies.

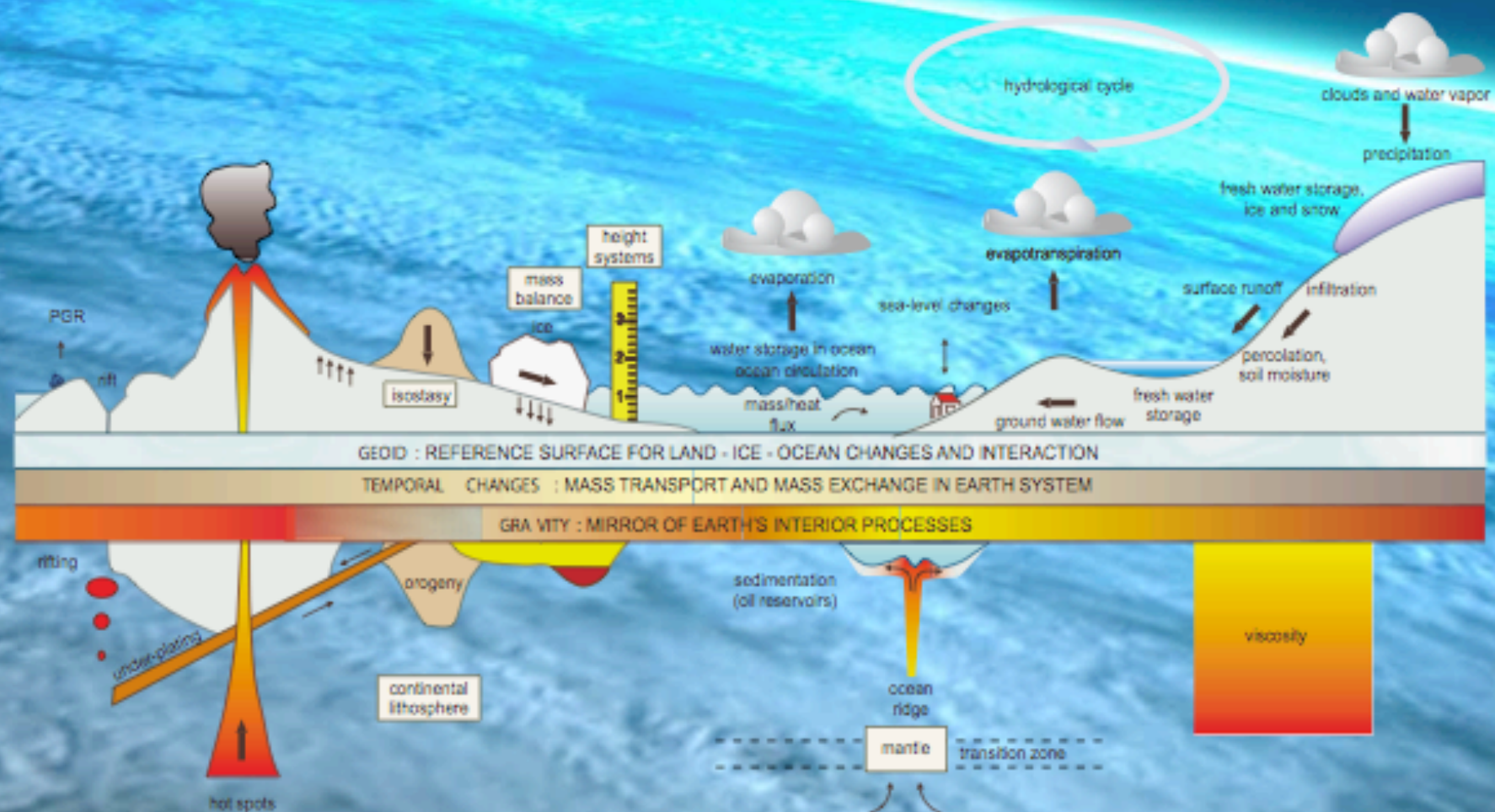


Mass redistribution in the Earth system. All geophysical processes are associated with mass redistribution and changes in the dynamics, thus affecting commonly the Earth's gravity field, geometry, and rotation. Consequently, space geodesy with observations of the "three pillars" contributes to an observing system that allows the monitoring of mass transport in the Earth system.

**GEODESY'S NEW CUSTOMERS**

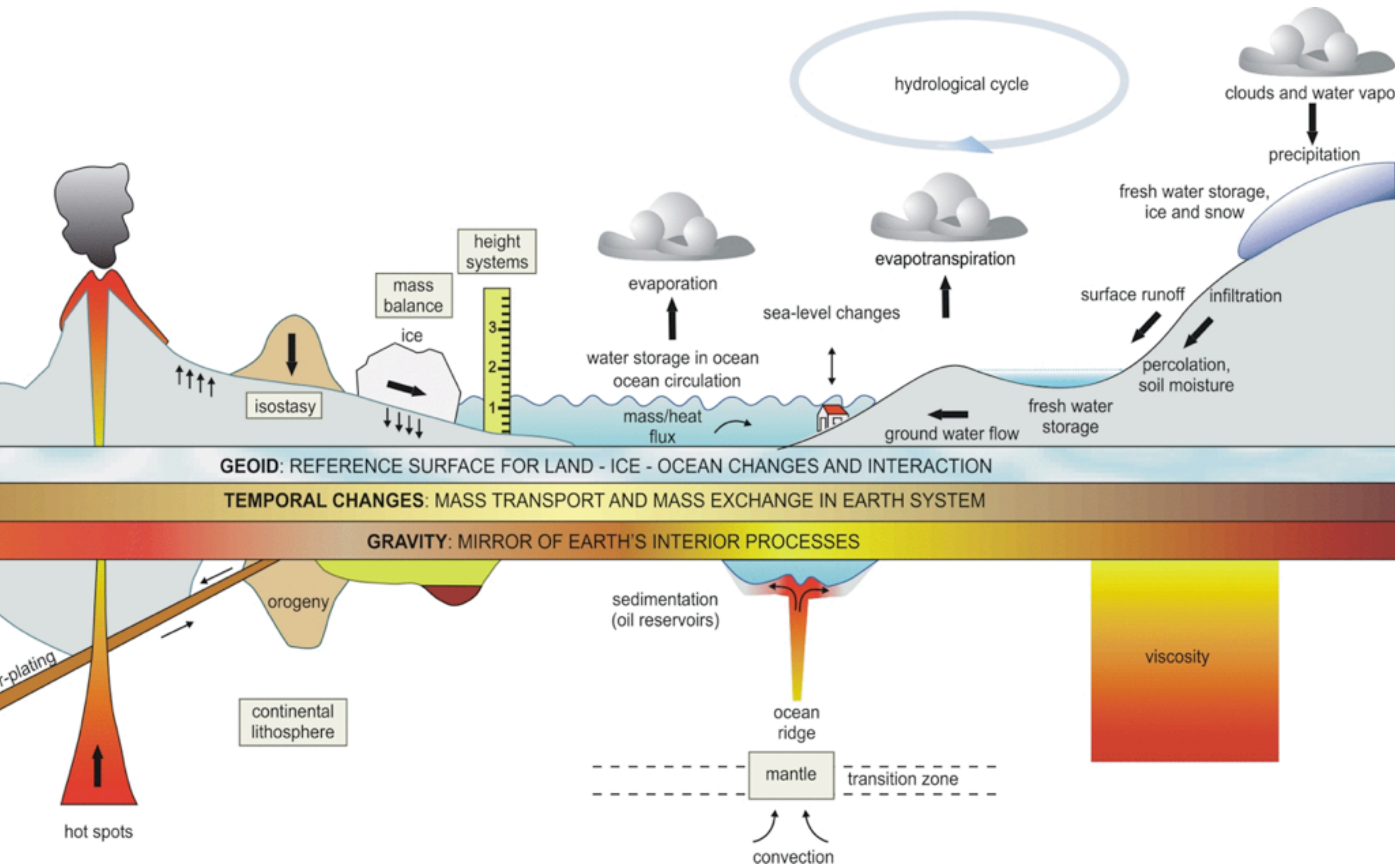
On a large extent, geodesy is a "service science". In the past, the main customers of geodesy came from the surveying and mapping profession, while today geodesy serves all Earth science, including the physical, oceanographic, atmospheric, and environmental science communities. Geodesy is also indispensable for the maintenance of infrastructure activities in a modern society. Traditionally, geodesy has served society by providing reference frames for a wide range of practical applications from regional to global navigation on land, sea, and in air, construction of infrastructure, to the determination of reliable boundaries of real estate properties. Reference frames were, however, national in scope, and they were suited for the determination of coordinates relative to a network of reference points. Thus, determination of precise point coordinates required simultaneous measurements at several points. Today, the Global Navigation Satellite Systems (GNSS) provide access to precise point coordinates in a global reference frame anytime and anywhere on the Earth's surface with centimeter-level accuracy and without requiring additional measurements on nearby reference points.

Geodesy has the potential to make very important contributions to the understanding of the state and dynamics of System Earth, particularly consistent observations of the "three pillars" can be provided on a global scale with a precision at or below the 1 ppb level, and with excellent stability over decades. A prerequisite to exploiting the full potential of geodesy for Earth observation, Earth system monitoring, and many practical applications is a sophisticated integration of all geodesy techniques (spaceborne, airborne, marine and terrestrial), process models and geophysical background models into one system. The realization of the "three pillars" will permit - as part of global change research - the assessment of surface deformation processes and the identification of mass anomalies and mass transport inside individual components, and mass exchange between the components of the Earth's system. These quantities serve as input to the study of the physics of solid Earth, ice sheets and glaciers, hydrosphere and atmosphere. Areas of particular value for the study of complex phenomena such as isostatic adjustment, the evolution of tectonic stress patterns, sea level rise and fall, the hydrological cycle, transport processes in the oceans, and the dynamics and physics of the atmosphere (troposphere and stratosphere).

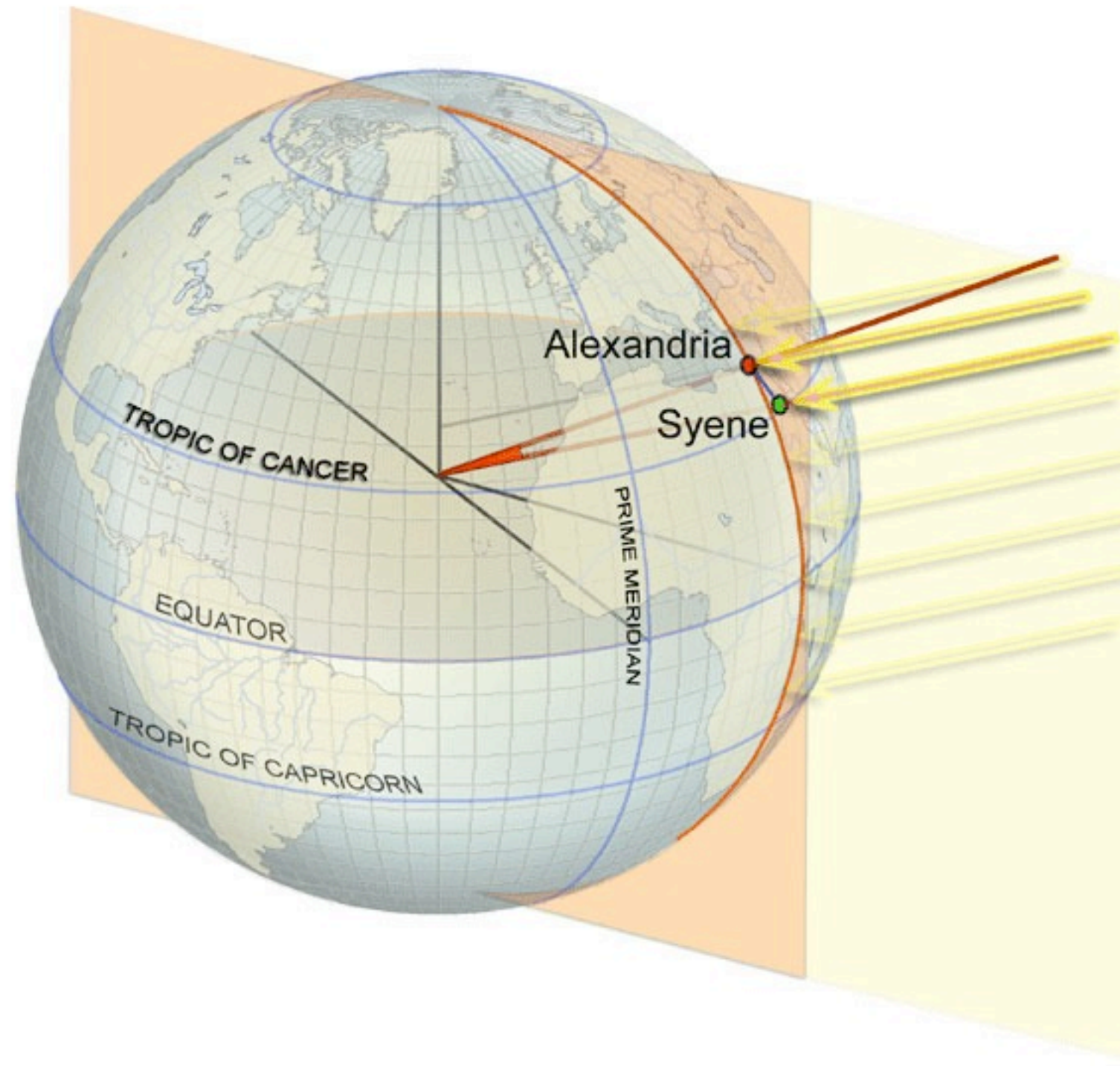




It can get a little complicated...



# Eratosthenes Estimates the Size of the Earth



from: <http://oceanservice.noaa.gov/education/kits/geodesy>

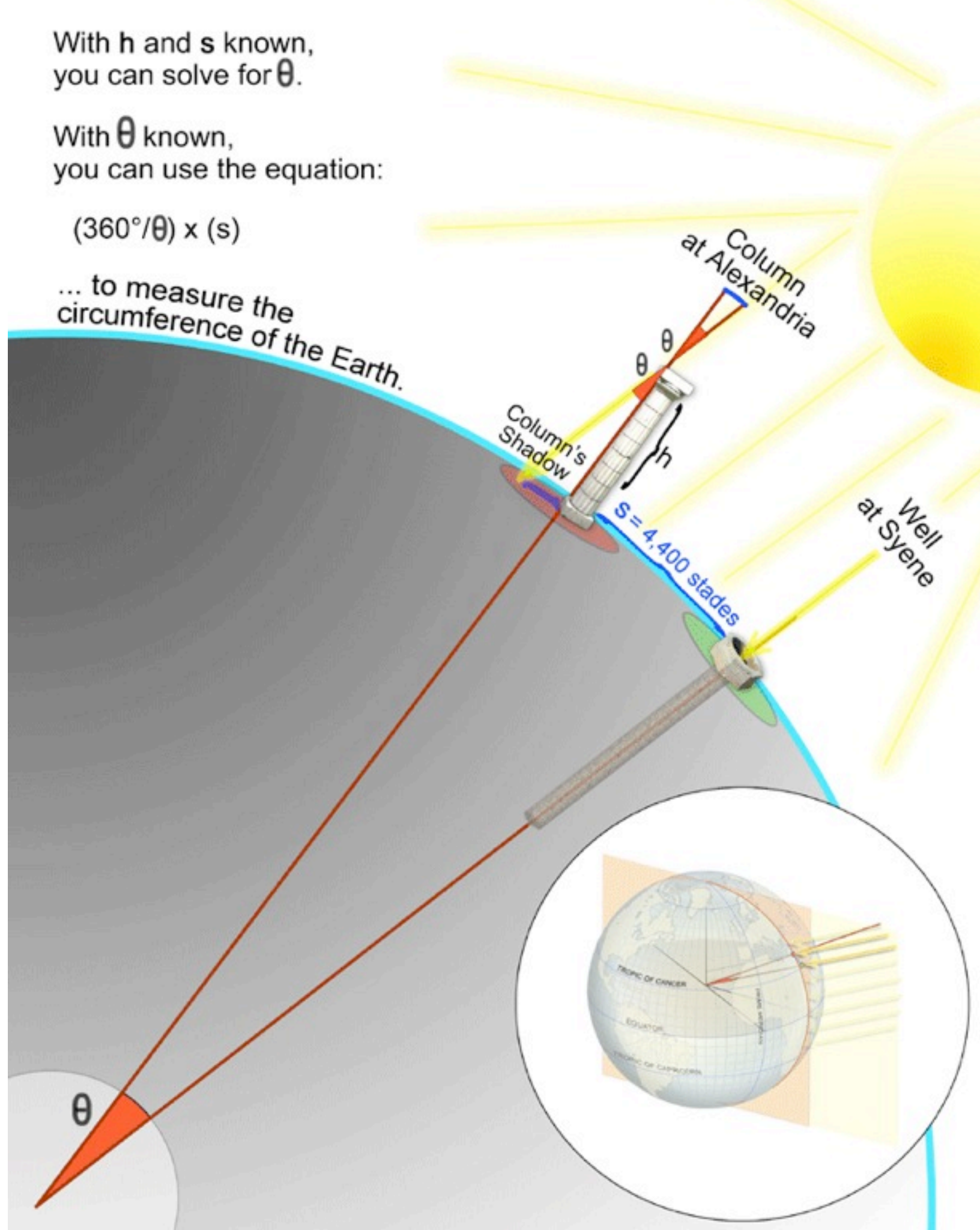


With  $h$  and  $s$  known,  
you can solve for  $\theta$ .

With  $\theta$  known,  
you can use the equation:

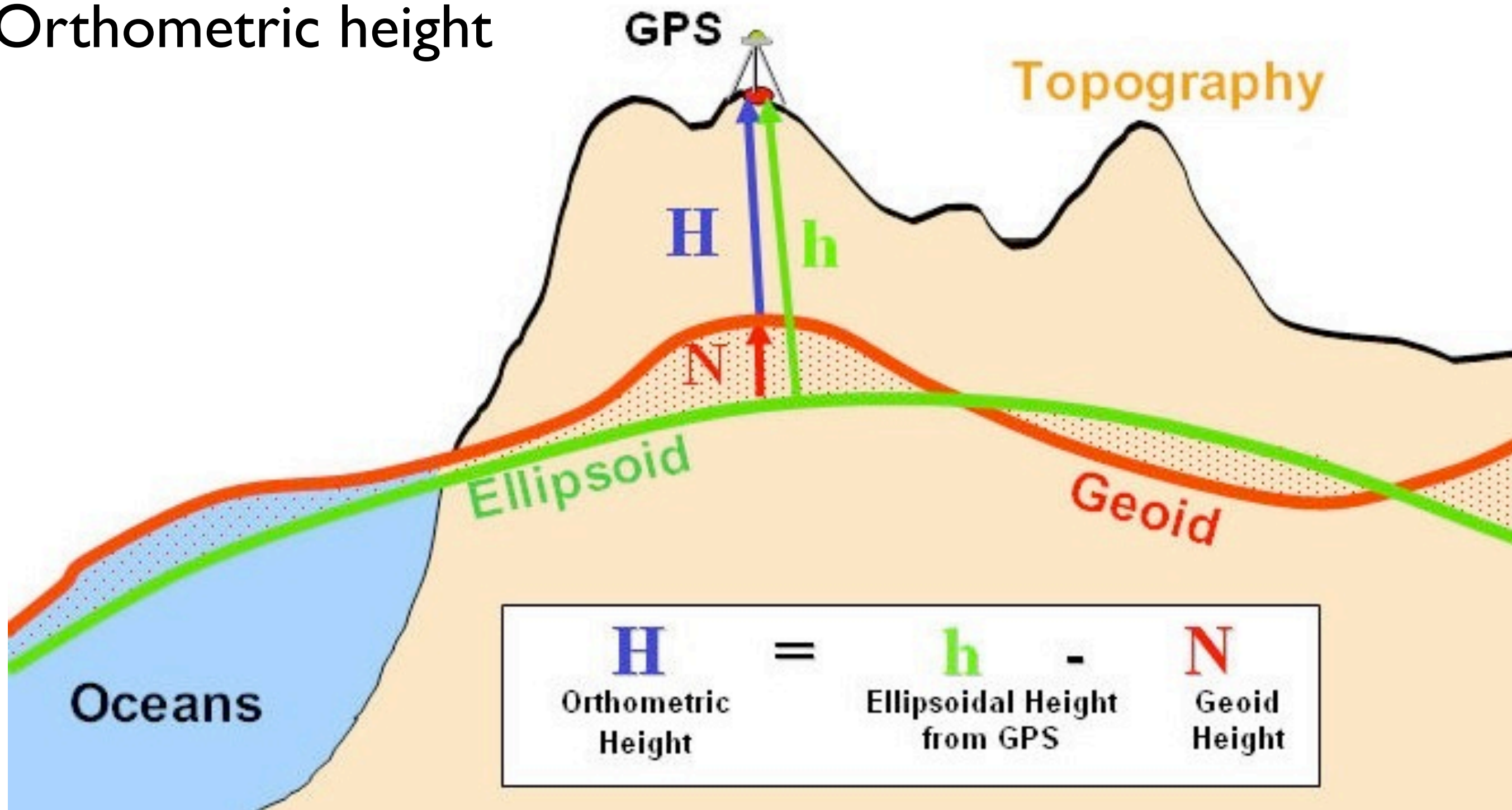
$$(360^\circ/\theta) \times (s)$$

... to measure the  
circumference of the Earth.



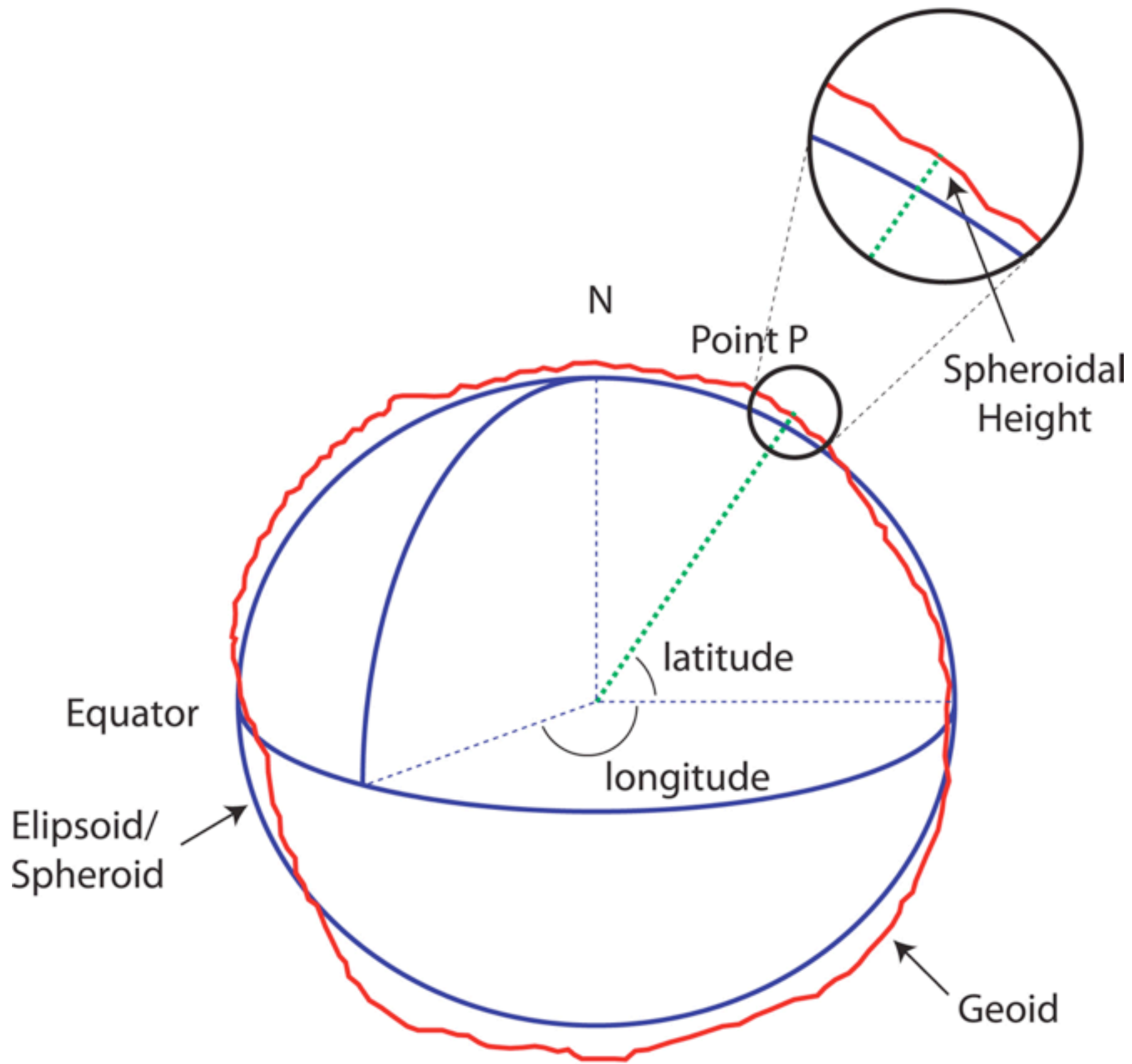
- He got a circumference of  $\sim 40,000$  km, error of near 2%.
- Lucky? Nobody really knows how big his 'stadia' were.
- Accounts of this story vary...

# Ellipsoidal height vs. Orthometric height



- What is height?
- Which direction is up?
- What is sea level?







At the 1967 meeting of the IUGG held in Lucerne, Switzerland, the ellipsoid called GRS-67 ([Geodetic Reference System 1967](#)) in the listing was recommended for adoption. The new ellipsoid was not recommended to replace the International Ellipsoid (1924), but was advocated for use where a greater degree of accuracy is required. It became a part of the GRS-67 which was approved and adopted at the 1971 meeting of the IUGG held in Moscow. It is used in Australia for the Australian Geodetic Datum and in South America for the South American Datum 1969.

Reference ellipsoid name	Equatorial radius (m)	Polar radius (m)	Inverse flattening	Where used
Modified Everest (Malaya) Revised Kertau	6,377,304.063	6,356,103.038993	300.801699969	
Timbalai	6,377,298.56	6,356,097.55	300.801639166	
Everest Spheroid	6,377,301.243	6,356,100.228	300.801694993	
<a href="#">Maupertuis</a> (1738)	6,397,300	6,363,806.283	191	France
<a href="#">Everest</a> (1830)	6,377,276.345	6,356,075.413	300.801697979	India
<a href="#">Airy</a> (1830)	6,377,563.396	6,356,256.909	299.3249646	Britain
<a href="#">Bessel</a> (1841)	6,377,397.155	6,356,078.963	299.1528128	Europe, Japan
<a href="#">Clarke</a> (1866)	6,378,206.4	6,356,583.8	294.9786982	North America
<a href="#">Clarke</a> (1878)	6,378,190	6,356,456	293.4659980	North America
<a href="#">Clarke</a> (1880)	6,378,249.145	6,356,514.870	293.465	France, Africa
<a href="#">Helmert</a> (1906)	6,378,200	6,356,818.17	298.3	
<a href="#">Hayford</a> (1910)	6,378,388	6,356,911.946	297	USA
International (1924)	6,378,388	6,356,911.946	297	Europe
<a href="#">NAD 27</a> (1927)	6,378,206.4	6,356,583.800	294.978698208	North America
<a href="#">Krassovsky</a> (1940)	6,378,245	6,356,863.019	298.3	Russia
<a href="#">WGS66</a> (1966)	6,378,145	6,356,759.769	298.25	USA/DoD
Australian National (1966)	6,378,160	6,356,774.719	298.25	Australia
New International (1967)	6,378,157.5	6,356,772.2	298.24961539	
GRS-67 (1967)	6,378,160	6,356,774.516	298.247167427	
South American (1969)	6,378,160	6,356,774.719	298.25	South America
<a href="#">WGS-72</a> (1972)	6,378,135	6,356,750.52	298.26	USA/DoD
<a href="#">GRS-80</a> (1979)	6,378,137	6,356,752.3141	298.257222101	
<a href="#">NAD 83</a>	6,378,137	6,356,752.3	298.257024899	North America
<a href="#">WGS-84</a> (1984)	6,378,137	6,356,752.3142	298.257223563	Global <a href="#">GPS</a>
<a href="#">IERS</a> (1989)	6,378,136	6,356,751.302	298.257	
<a href="#">IERS</a> (2003) <sup>[2]</sup>	6,378,136.6	6,356,751.9	298.25642	Global <a href="#">ITRS</a>

# Datums



# The Geoid

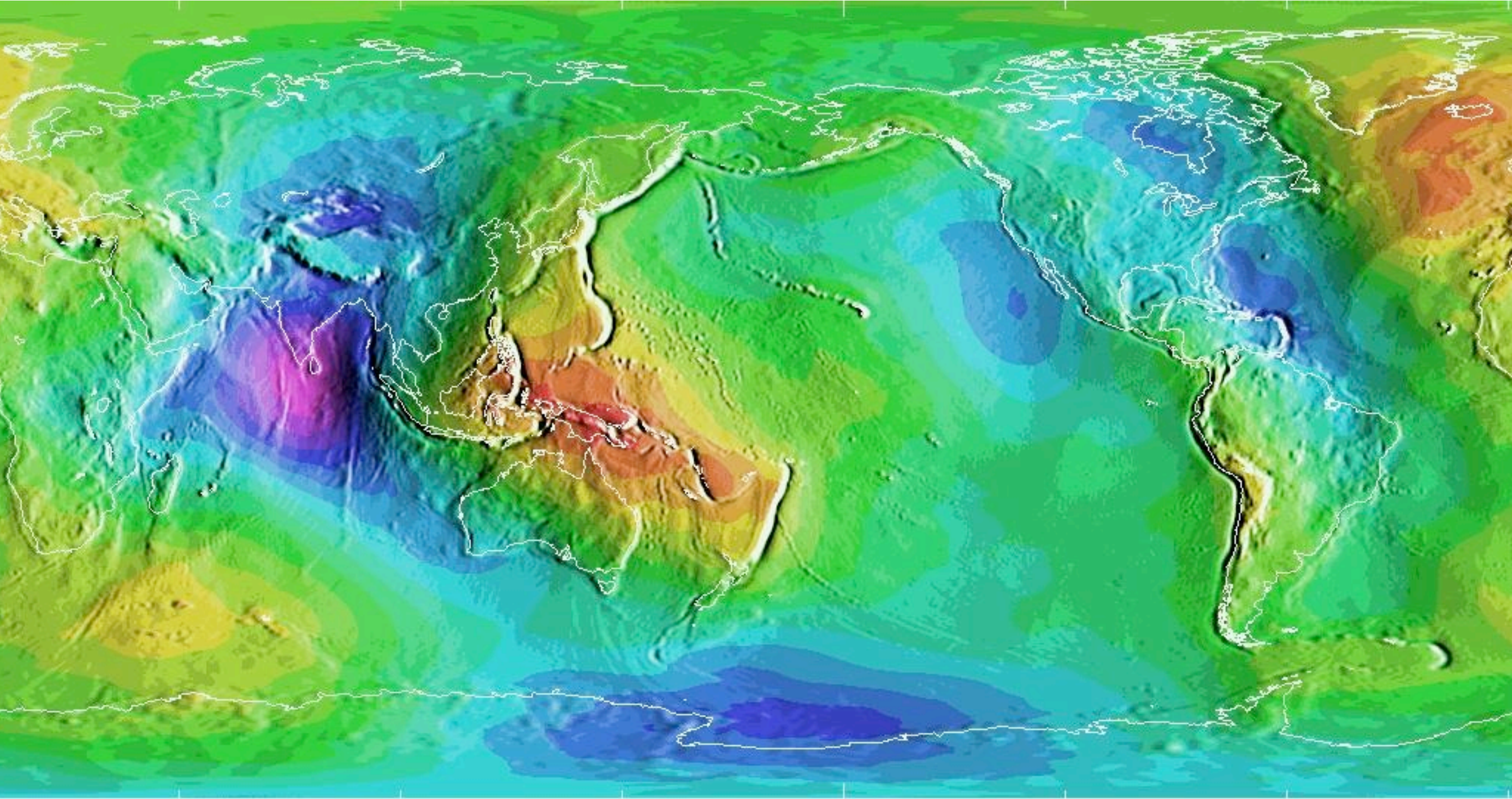
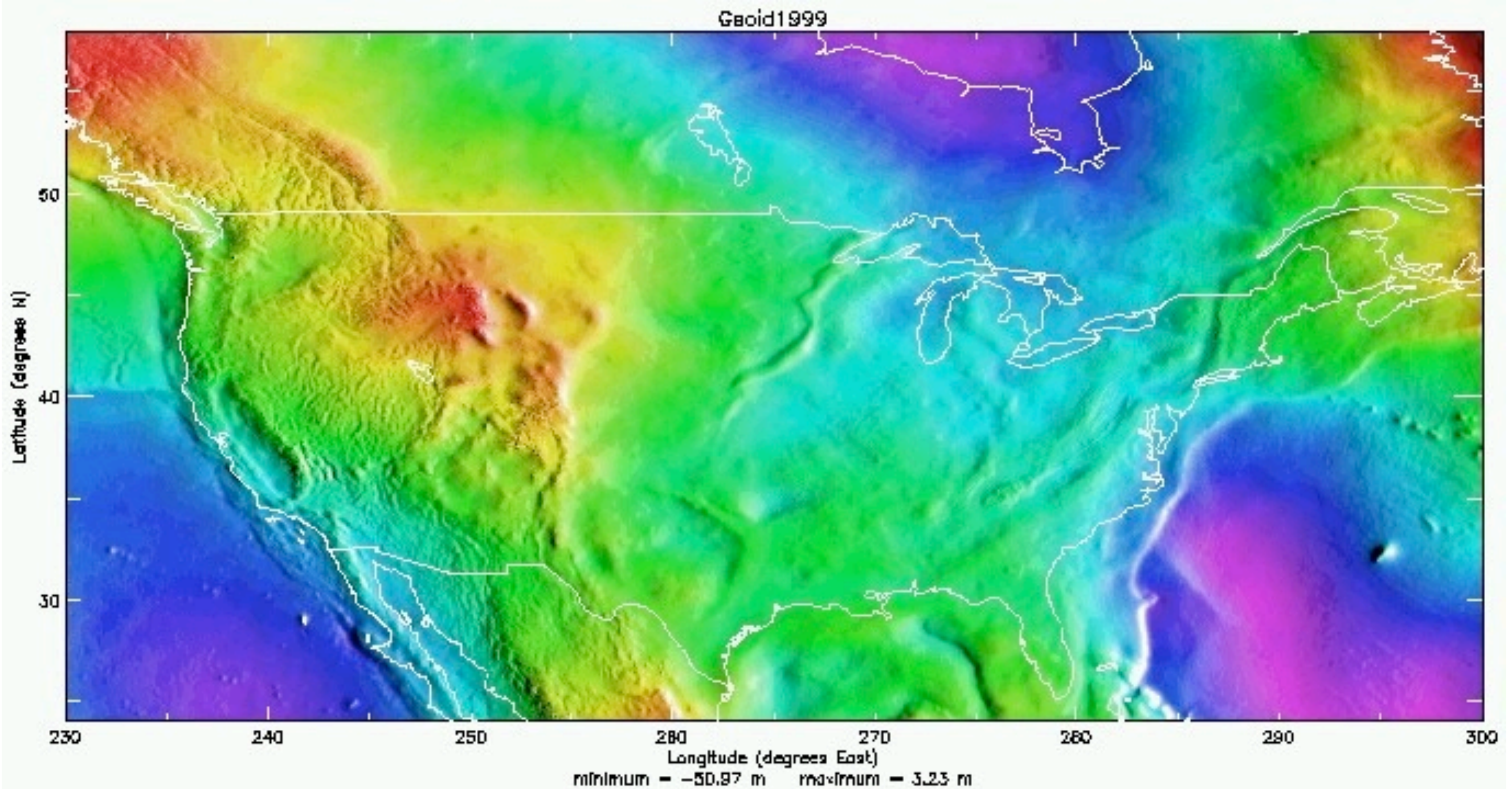


Image Name : ww15mgh; Boundaries : Lat -90N to 90N; Lon 0E to 360E;  
Color Scale, Upper (Red) : 85.4 meters and higher; Color Scale, Lower (Magenta) :-107.0 meters and lower  
Data Max value : 85.4 meters Data Min value :-107.0 meters Illuminated from the : East

figure taken from [http://principles.ou.edu/earth\\_figure\\_gravity/geoid/index.html](http://principles.ou.edu/earth_figure_gravity/geoid/index.html)





*GEOID99 is a refined model of the geoid in the United States, which supersedes the previous models GEOID90, GEOID93, and GEOID96. For the conterminous United States (CONUS), GEOID99 heights range from a low of -50.97 meters (magenta) in the Atlantic Ocean to a high of 3.23 meters (red) in the Labrador Strait. However, these geoid heights are only reliable within CONUS due to the limited extents of the data used to compute it. GEOID99 models are also available for Alaska, Hawaii, and Puerto Rico & the U.S. Virgin Islands.*

See also: Smith, D. A., and D. R. Roman (2001), GEOID99 and G99SSS: 1-arc-minute geoid models for the United States, *Journal of Geodesy*, 75, 469-490.

# Vertical Land Motion (VLM) and Local Sea Level (LSL)

## Local Sea Level (LSL)

- as measured by tide gauges
- relevant to coastal impacts

## Geocentric Sea Level (GSL)

- sea surface height: altimeters
- relative to ITRF origin
- CM(Earth)  $\pm$  0.5 mm/yr

## Vertical Land Motion (VLM)

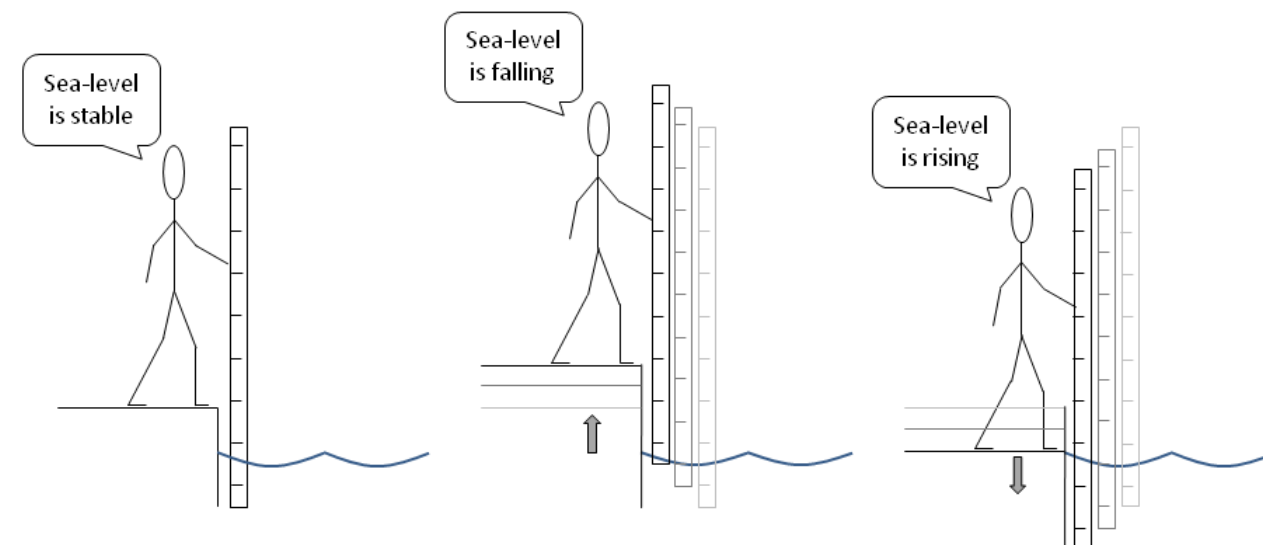
$$\text{LSL} = \text{GSL} - \text{VLM}$$

- GSL & VLM relative to ITRF

## Coastal subsidence (-VLM)

- Obviously 1:1 effect on LSL

### Stating the Obvious



Source: P. Whitehouse  
<http://www.antarcticglaciers.org/recovering-from-an-ice-age>



# Practical Matters

Sea level rise affects coastal areas

Piazza San Marcos,  
Venice Italy

Some areas have special sensitivity













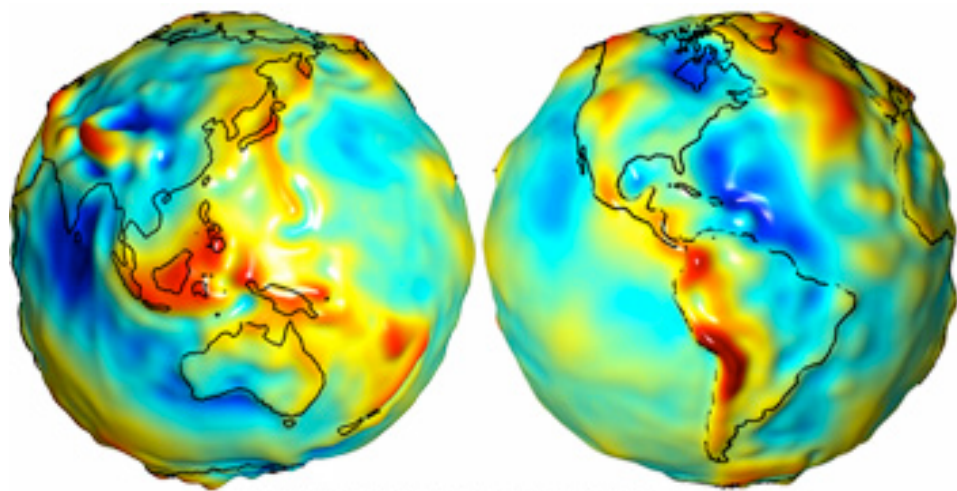




# The Point

- Global sea level rise ongoing at the level of  $\sim 1$  mm/yr. Contributions from melting of ice and steric (temperature and salinity) of oceans.
- Regional variations owing to different mechanisms behind sea level increase
- Coastal subsidence (vertical motion of the ground) exacerbates effects of local sea level rise
- Earth shape changes at local, global levels can contribute to site specific effects.
- Venice going down at  $\sim 1$  mm/yr wrt Earth Center of Mass.



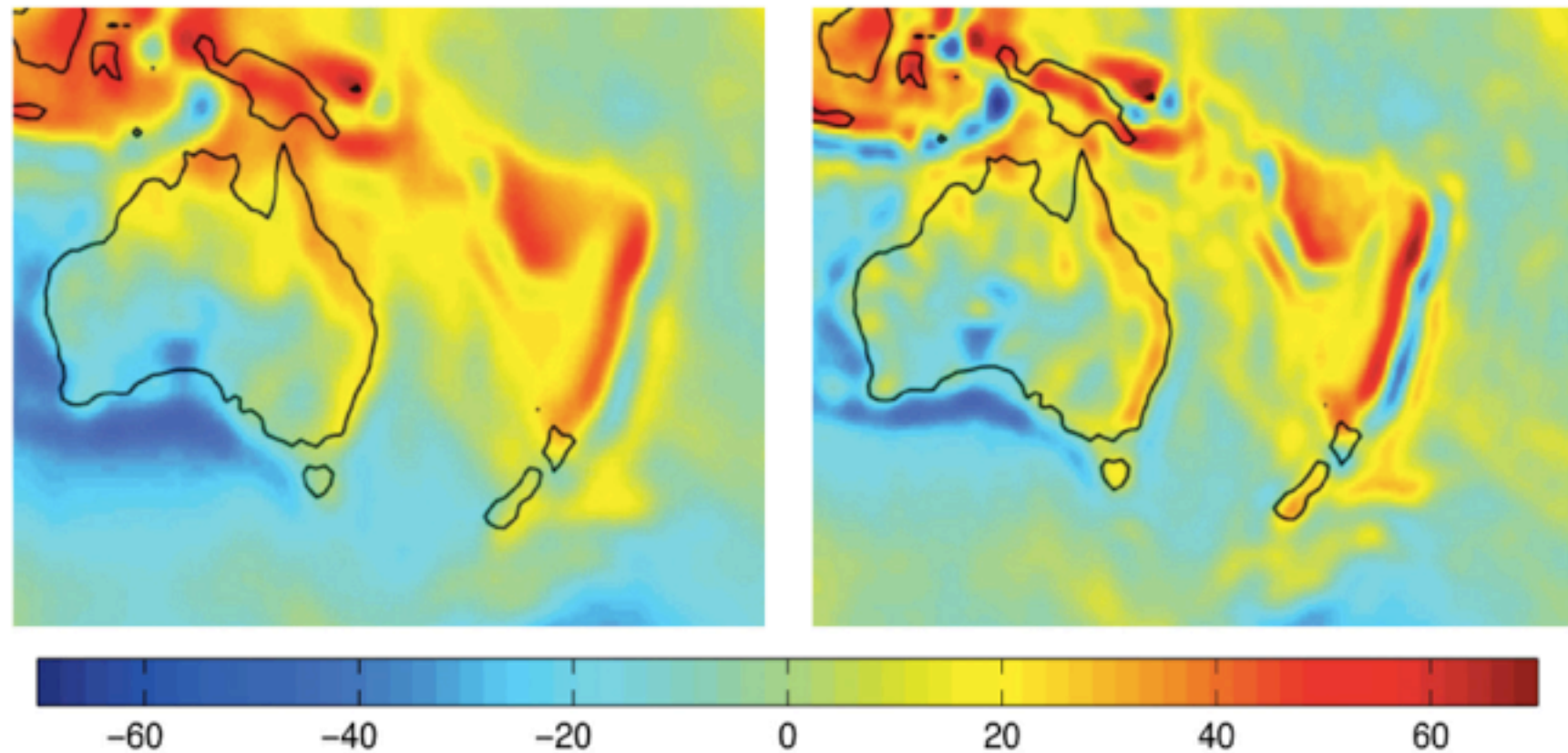


Earth's Gravity Field Anomalies (milligals)  
 -50 -40 -30 -20 -10 0 10 20 30 40 50

# Gravity anomalies



## GRACE

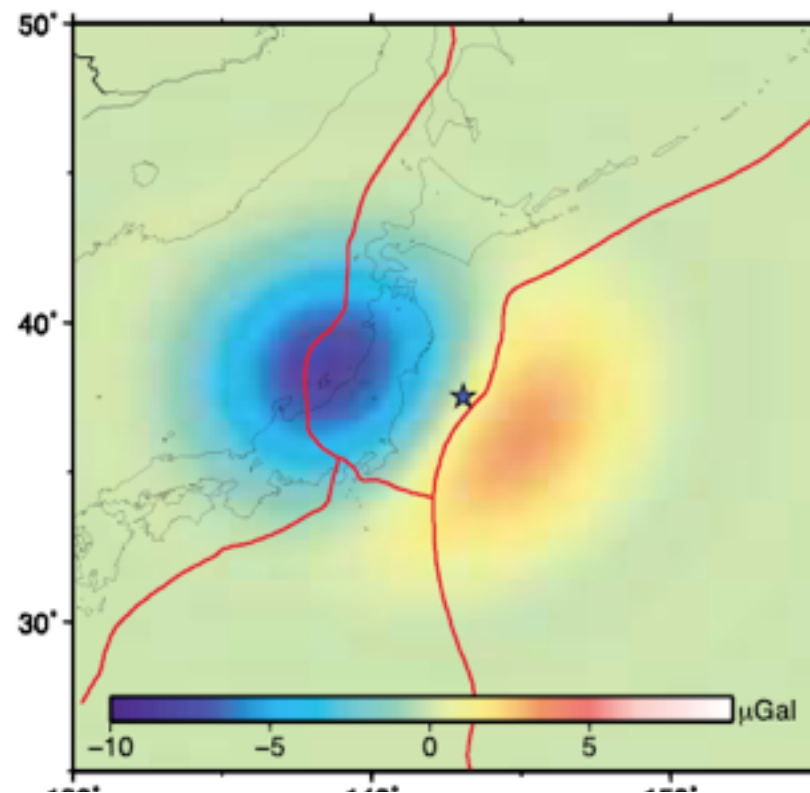


**Figure 3.** Improvement in resolution in gravity anomalies computed from GGM02S (right) compared to GGM01S (left) in the Tonga-Kermadec. With the increased accuracy of the GGM02S model, less smoothing is required to remove artifacts and more detail is revealed. Units are mgal.

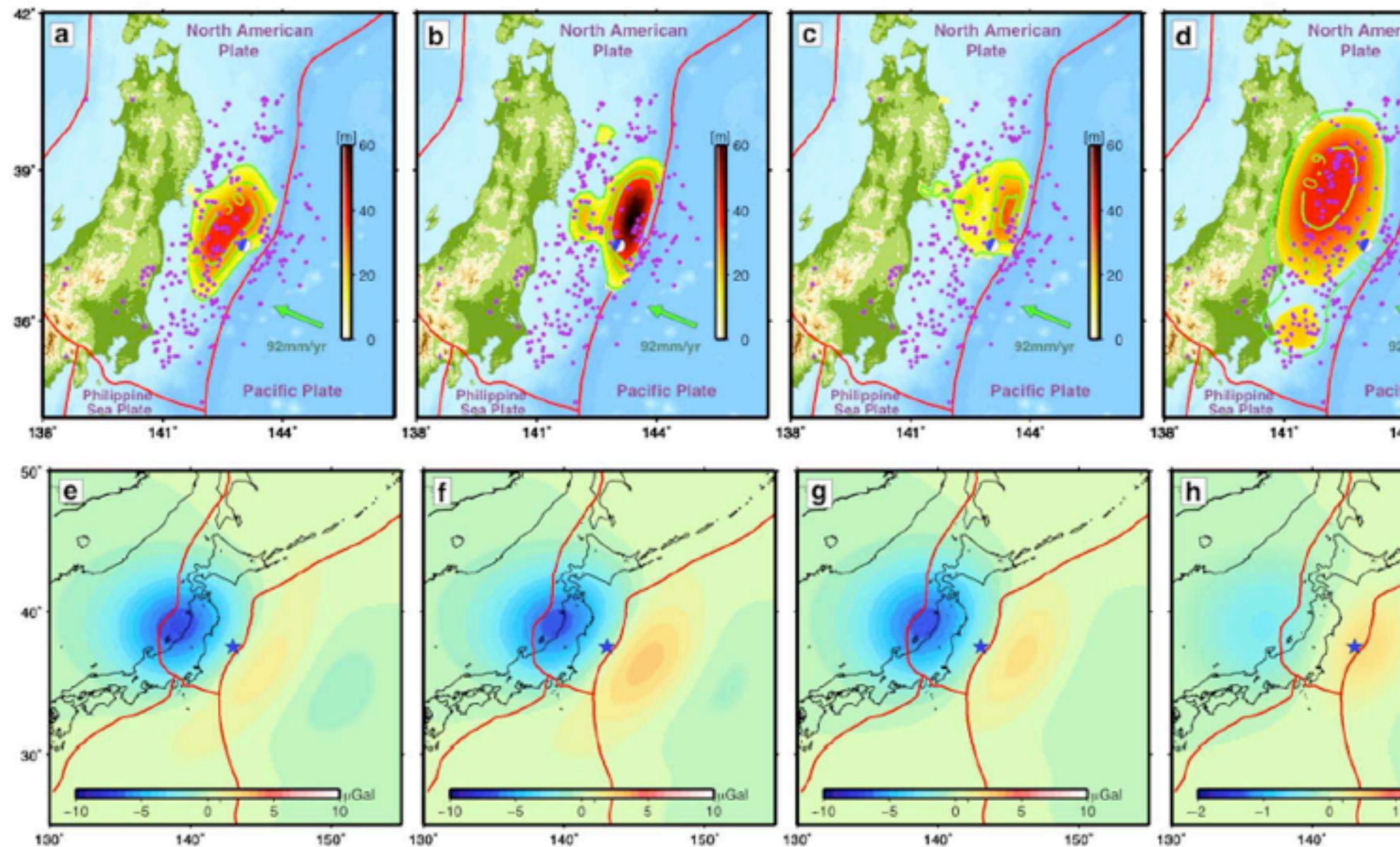


# Tohoku 2011 M 9.0 Earthquake

Observed from GRACE



Predicted from  
Slip Models

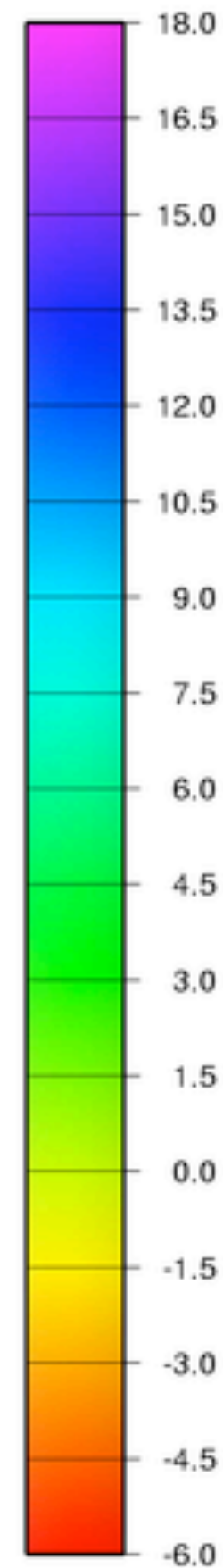
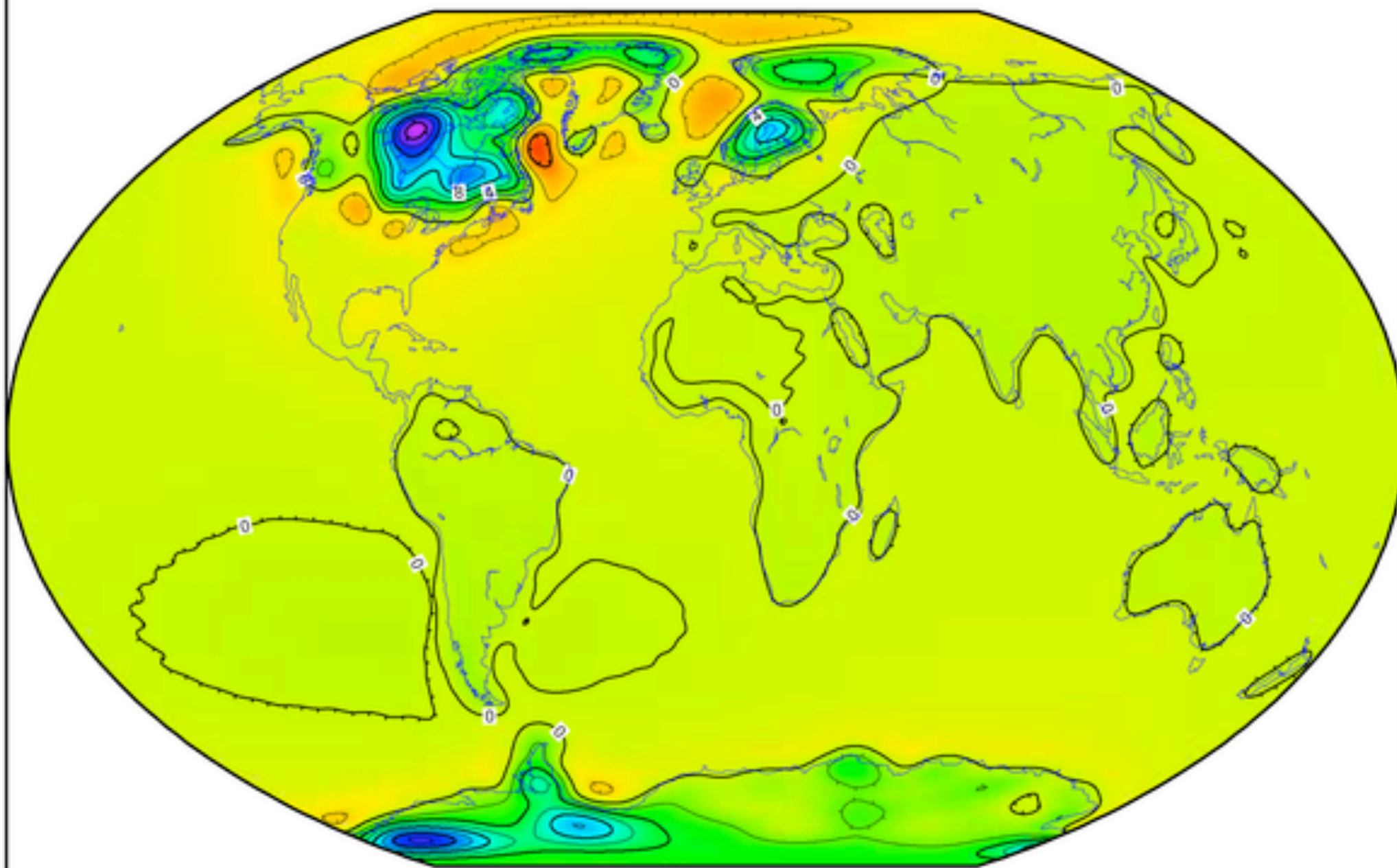




# How Big Are These Gravity Variations?

- In previous figure gravity varied by  $\sim 100$  mgals =  $0.1$  gals =  $0.1$  cm/s<sup>2</sup> =  $.001$  m/s<sup>2</sup>
- Acceleration owing to Earth's surface gravity field is near  $9.8$  m/s<sup>2</sup>
- Variation in gravity is around 1 part in  $10^4$  (.01%)

vertical crustal motions in mm per year via GIA theory



Paulson et al., 2007



# Plate Tectonic Significance of The Gravity Field

- Equation from Coblentz et al.
- Equation from Turcotte & Schubert
- Can estimate variations in gravitational potential energy in the lithosphere
- Which can be used to estimate state of stress in the lithosphere owing to gravity forces.
- Which can be combined with plate boundary stress estimates to estimate stress on edges of the plates.



## On the gravitational potential of the Earth's lithosphere

David D. Coblenz and Randall M. Richardson

Southern Arizona Seismic Observatory, Department of Geosciences, University of Arizona, Tucson

Michael Sandiford

Department of Geology and Geophysics, University of Adelaide, Adelaide, Australia

## Gravitational Potential Energy of the Lithosphere

The gravitational potential energy per unit area of a column of material  $U$  above a given depth  $z$  is given by the integral of the vertical stress  $\sigma_{zz}$  from  $z$  to the surface  $h$  [e.g., *Molnar and Lyon-Caen, 1988*]

$$U = \int_z^h \sigma_{zz}(\tau) d\tau = g \int_z^h \int_\tau^h \rho(\tau') d\tau' d\tau \quad (1)$$

where  $\rho(z)$  is the density at depth  $z$ ;  $h$  is the surface elevation; and  $g$  is the gravitational acceleration. The potential energy of the lithospheric column  $U_l$  is defined by (1) when  $z$  corresponds to the equipotential surface at which the lithosphere is compensated  $z_{iso}$ . For the purpose of this study it is useful to define the mean potential energy of the lithosphere at both the global scale  $\overline{U_l^g}$  and the plate scale  $\overline{U_l^p}$ .

Because the lithosphere can be considered to be in isostatic equilibrium for wavelengths greater than a few hundred kilometers [*Kaula, 1970, 1972; Turcotte and McAdoo, 1979; Sandwell and Smith, 1992*], horizontal stresses can be directly related to the vertical density distribution [*Haxby and Turcotte, 1978; Dahlen, 1981*]

$$\overline{\sigma_{xx}} = \frac{g}{L} \int_h^L \Delta \rho(z) z dz \quad (2)$$

where  $z$  is the depth;  $L$  is the lithospheric thickness; and  $\overline{\sigma_{xx}}$  is the horizontal stress averaged over the thickness of the lithosphere, relative to a reference state against which the  $\Delta \rho$  is measured. Equation (2) shows that the mean horizontal stress is related to the local dipole moment of the density distribution  $M$

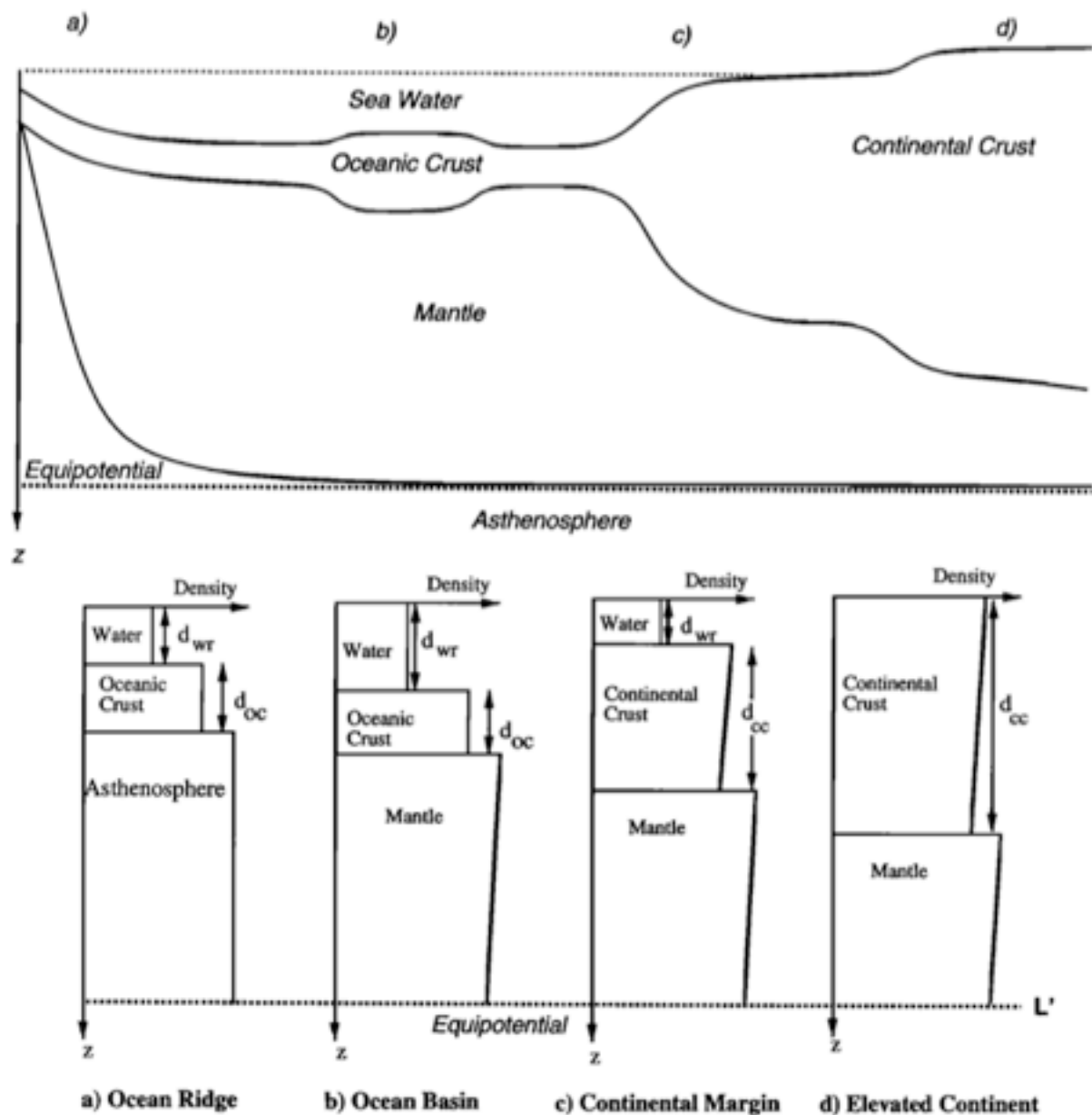
$$\overline{\sigma_{xx}} = \frac{g}{L} M \quad (3)$$

Using the definition of gravitational potential energy in (1), the horizontal stress can be expressed in terms of the potential energies

$$\overline{\sigma_{xx}} = \frac{\Delta U_l}{L} \quad (4)$$

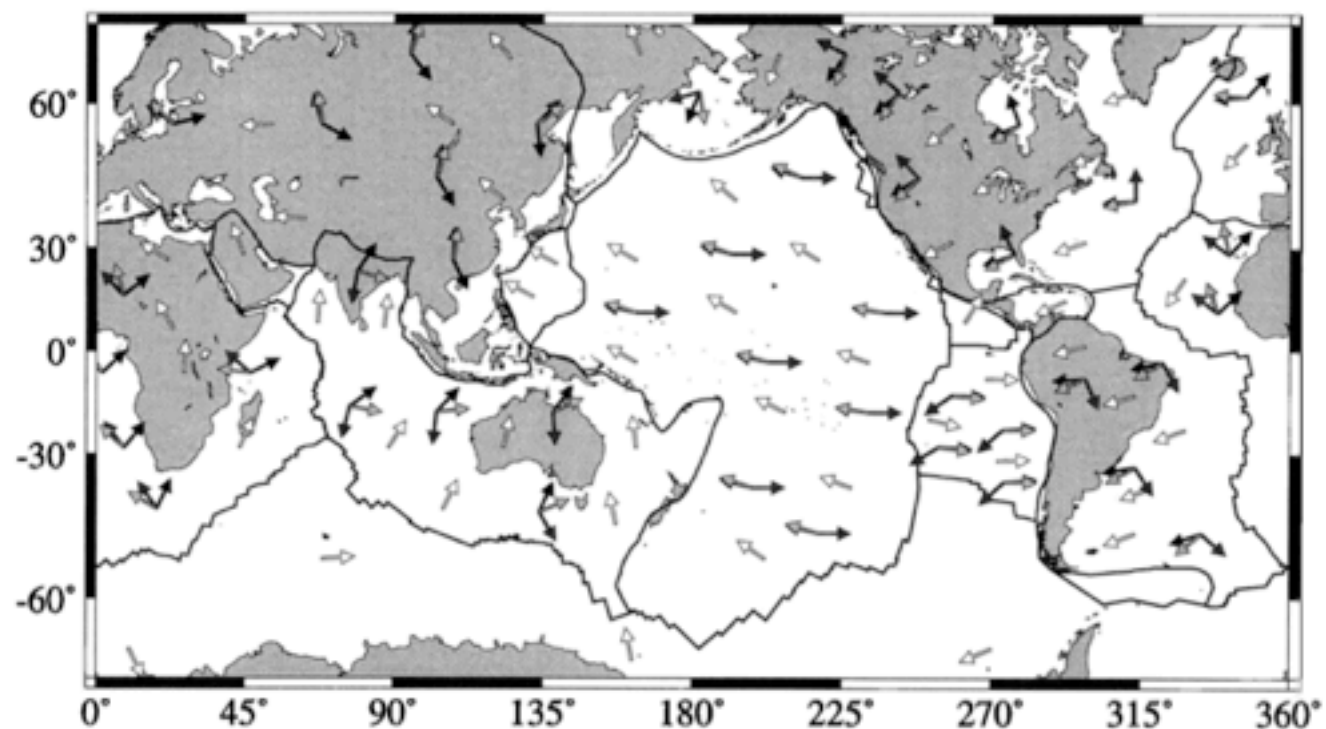
where  $\Delta U_l$  is the difference between the potential energy of the local lithospheric column  $U_l$  and the poten-





**Figure 1.** Schematic of the lithospheric depth-density distributions for the four lithospheric types: (a) ocean ridge, (b) oceanic basin, (c) continental margin, and (d) elevated continent. The density of the continental crust and mantle lithosphere varies as a linear function with depth. See text for details.

Normalized



**Figure 6.** Comparison of ridge torque (solid arrows), topographic torque (medium gray shaded arrows), potential energy torque (light grey shaded arrows), and absolute velocity directions (open arrows) for the seven major plates. The magnitude of the torques and velocity vectors have been normalized to unit length. Plate velocity information is from *Minster and Jordan* [1978] for the Indo-Australian plate and from *NUVEL-1* [Griffiths and Gordon, 1990] for all other plates. The Pacific ridge and total torque arrows nearly coincide because the total torque acting on the plate is dominated by the ridge torque.

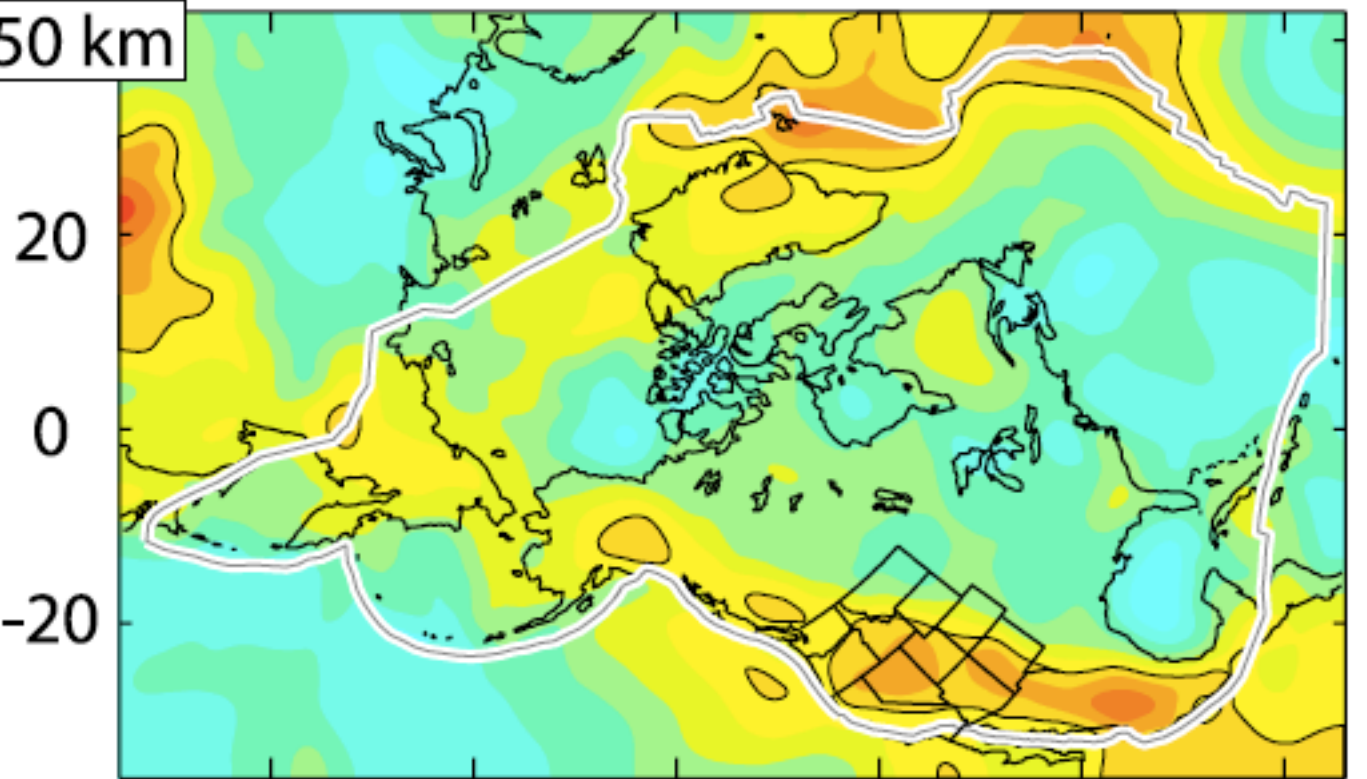
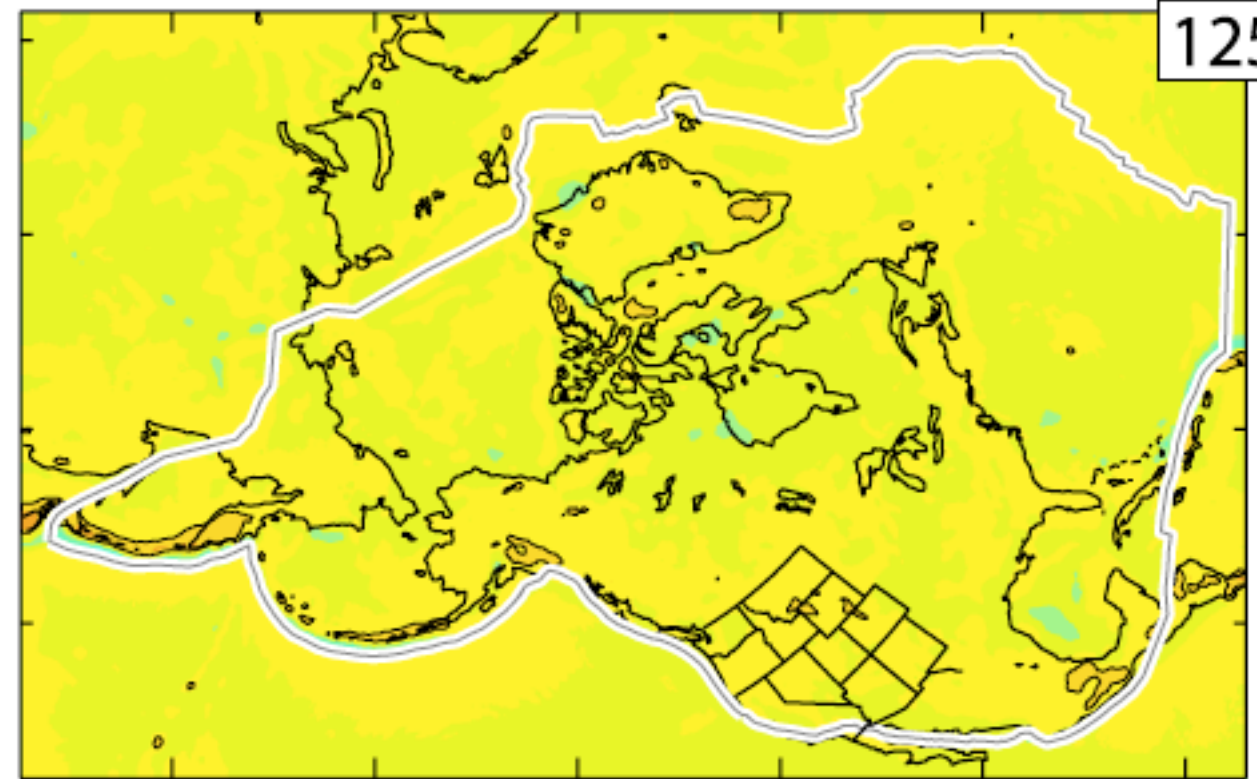


PE from geoid

PE from CRUST 2.0

b

1250 km

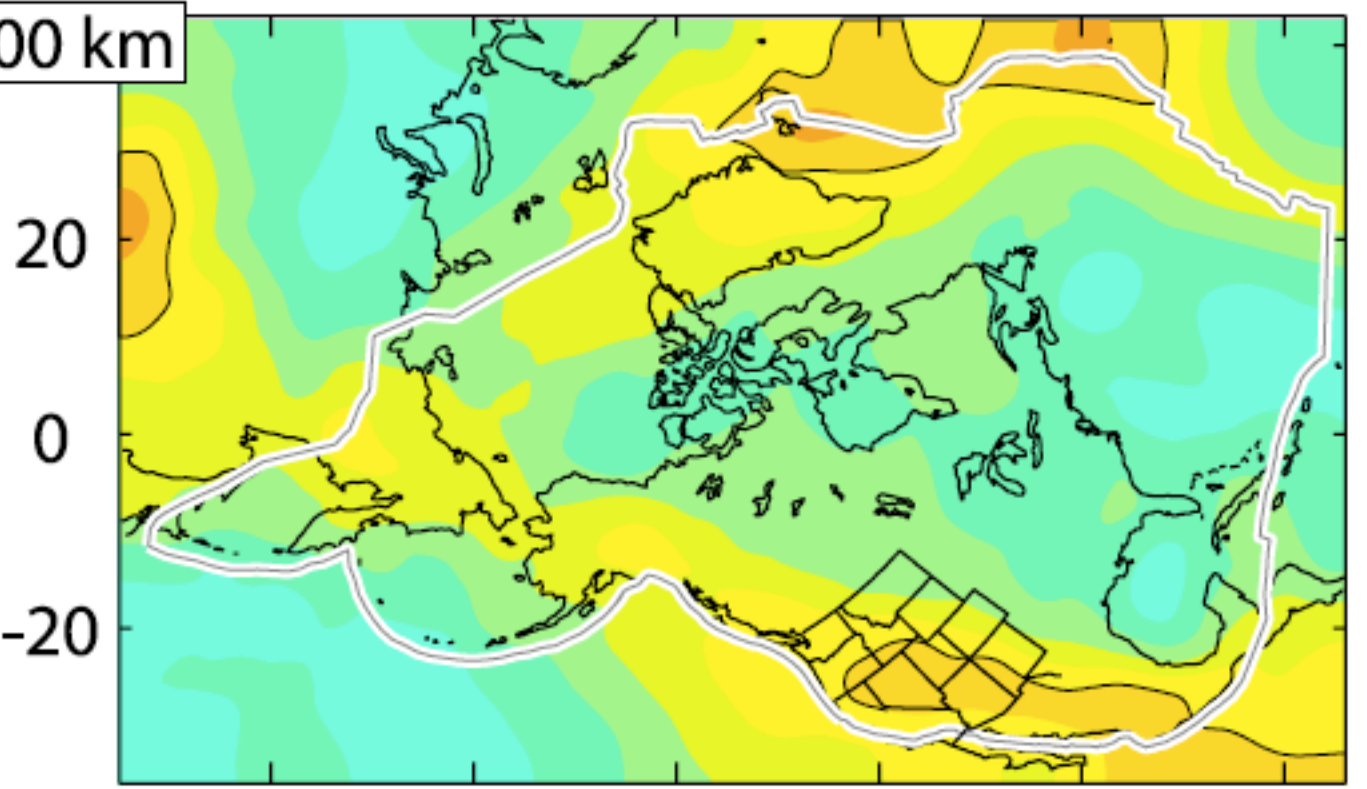
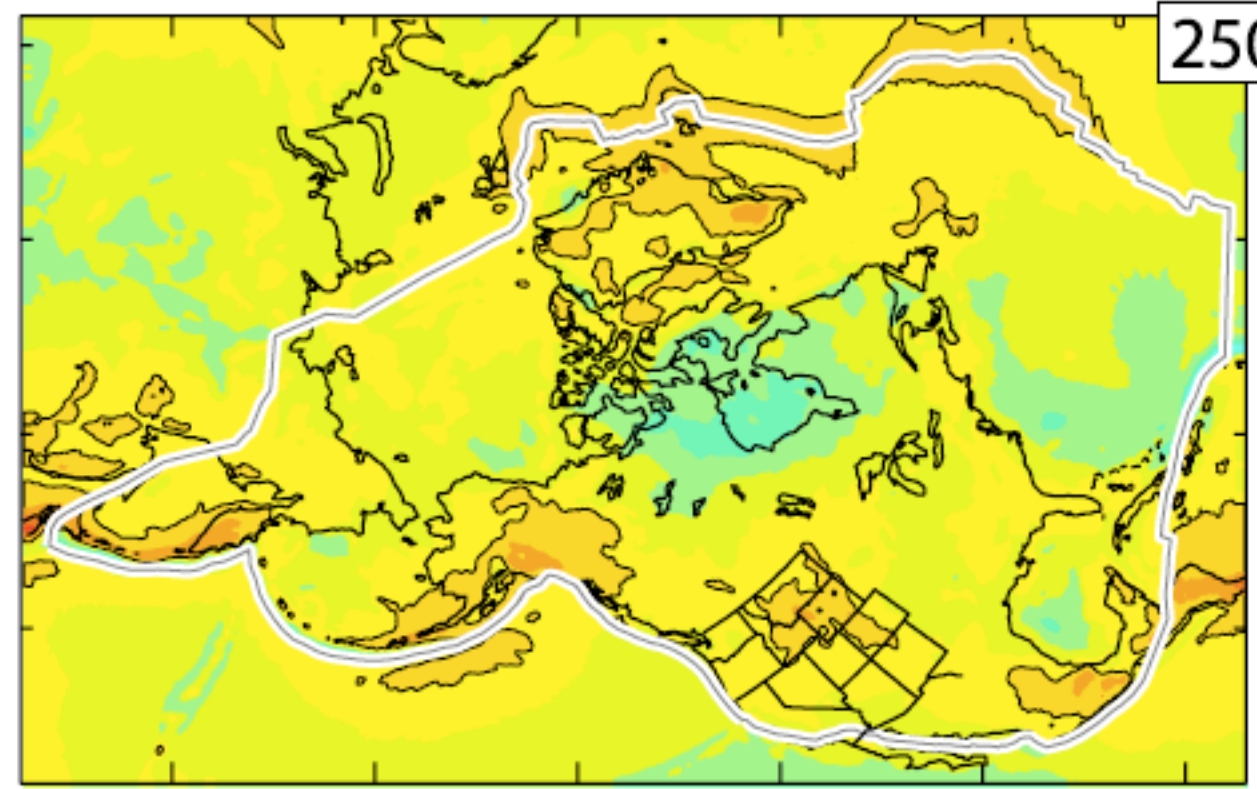


20

0

-20

2500 km

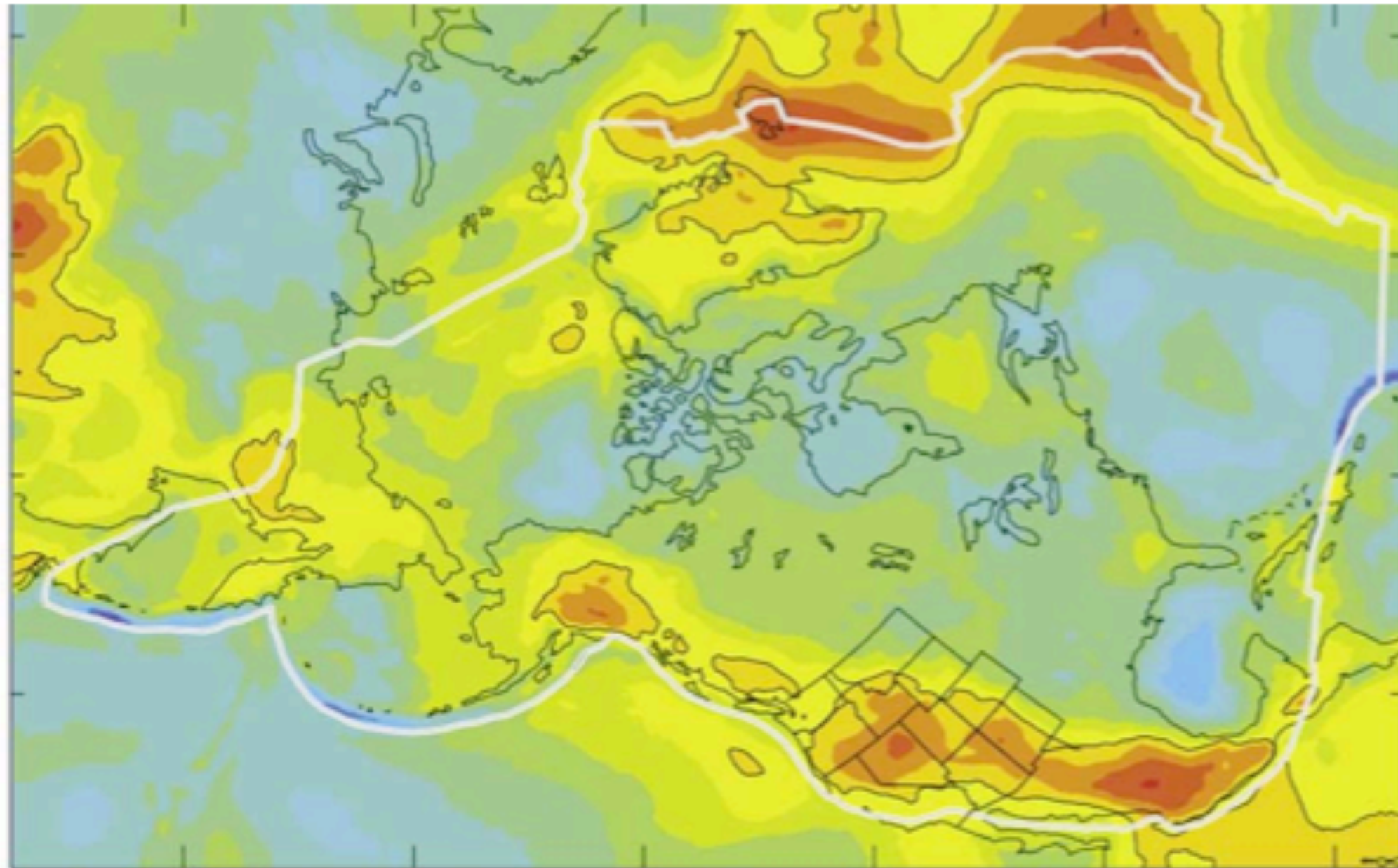


20

0

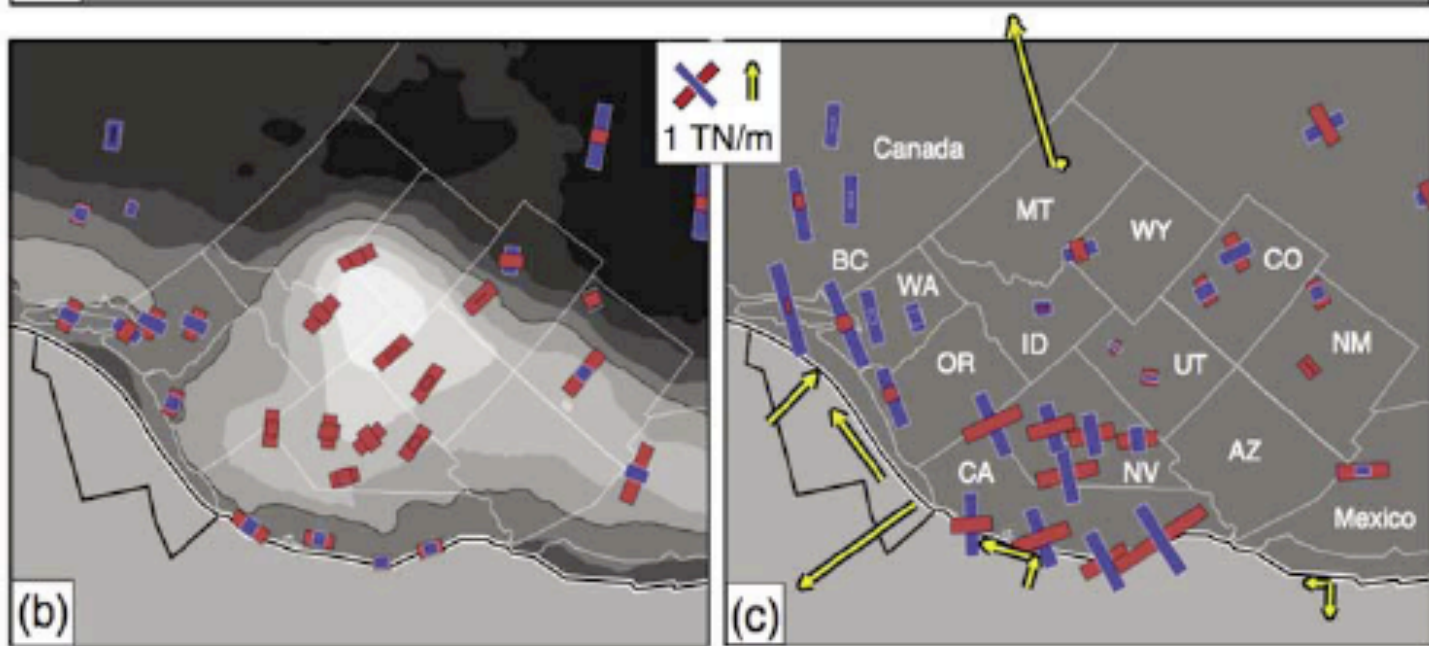
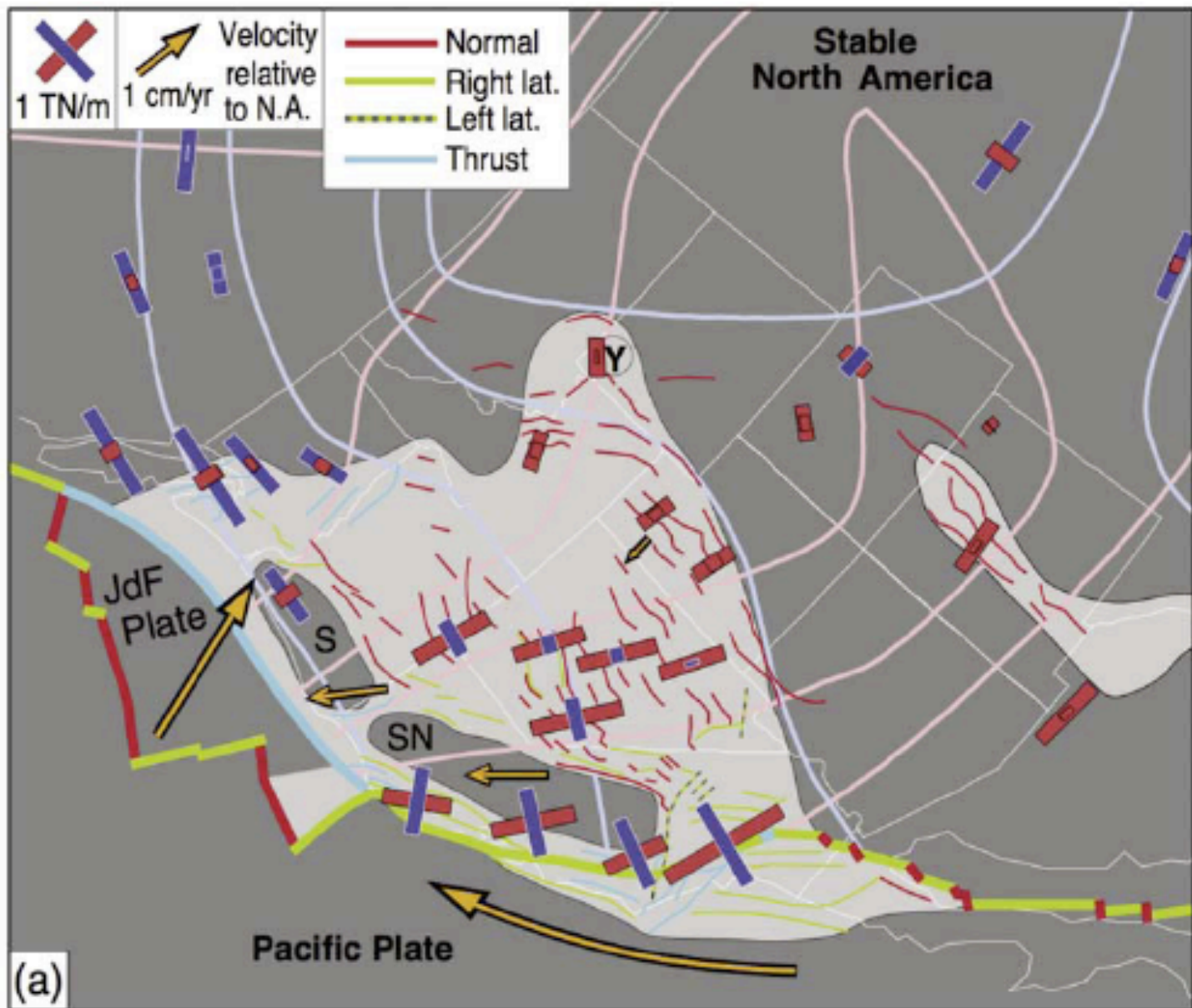
-20





**Figure 5.** Estimated total gravitational potential energy relative to reference ridge (black contour) (Table A2), as discussed in Appendix A. Contour level is 1 TN/m. This is the same image as the top right plot in Figure A2.





Humphreys and Coblenz, 2007